

# From Neural Networks to the Intelligent Power Grid: What It Takes to Make Things Work

- What is an Intelligent Power Grid, and why do we need it?
- Why do we need neural networks?
- How can we make neural nets really work here, & in diagnostics/"prediction"/"control" in general?

# What is a Truly Intelligent Power Grid?

- **True intelligence** (like brain)  $\Rightarrow$  **foresight**,  $\Rightarrow$  ability to learn to coordinate all pieces, for **optimal** expected performance on the bottom line in future despite random disturbances.
- Managing complexity is easy– if you don't aim for best possible performance! The challenge is to come as close as possible to **optimal performance of whole system**.
- Bottom line utility function includes value added, quality of service (reliability), etc. A general concept. Nonlinear robust control is just a special case.
- Enhanced communication/chips/sensing/actuation/HPC needed for max benefit(cyberinfrastructure, EPRI roadmap)
- Brain-like intelligence = embodied intelligence,  $\neq$  **AI**

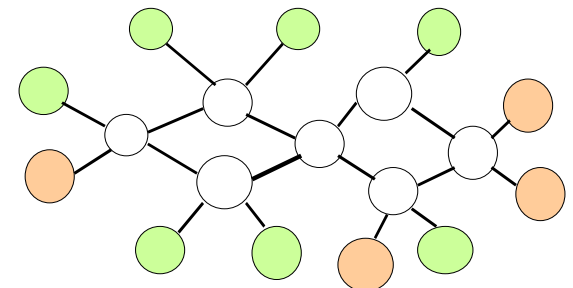


# Dynamic Stochastic Optimal Power Flow (DSOPF): How to Integrate the “Nervous System” of Electricity

- DSOPF02 started from EPRI question: can we optimally manage&plan the whole grid as **one** system, with foresight, etc.?
- Closest past precedent: Momoh’s OPF integrates &optimizes many grid functions – but deterministic and without foresight. UPGRADE!
- ADP math required to add foresight and stochastics, critical to more complete integration.

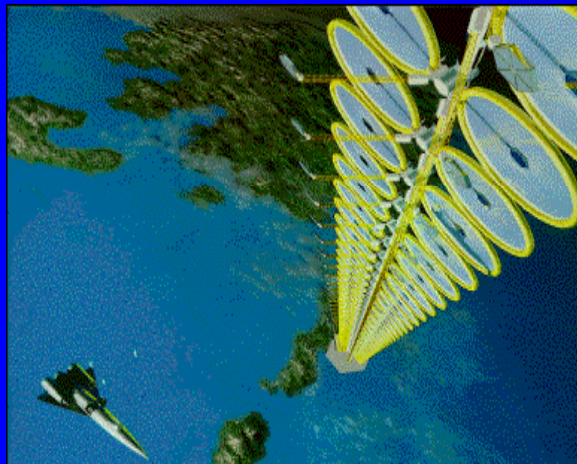


## ANN to I/O From Idealized Power Grid



- ❏ 4 General Object Types (busbar, wire, G, I)
- ❏ Net should allow **arbitrary number** of the 4 objects
- ❏ How design ANN to input and output FIELDS -- variables like the SET o values for current ACROSS all objects?

# Why It is a Life-or-Death Issue



HOW?



- [www.ieeeusa.org/policy/energy\\_strategy.ppt](http://www.ieeeusa.org/policy/energy_strategy.ppt)
- Photo credit IEEE Spectrum

As Gas Prices  $\uparrow$  Imports  $\uparrow$  & Nuclear Tech in unstable areas  $\uparrow$ , **human extinction** is a serious risk. Need to **move faster**.

Optimal time-shifting – big boost to rapid adjustment, \$

# Why It Requires Artificial Neural Networks (ANNs)

- For optimal performance in the general nonlinear case (nonlinear control strategies, state estimators, predictors, etc...), we need to adaptively estimate nonlinear functions. Thus we must use **universal nonlinear function approximators**.
- Barron (Yale) proved basic ANNs (MLP) **much better** than Taylor series, RBF, etc., to approximate smooth functions of many inputs. Similar theorems for approximating dynamic systems, etc., especially with more advanced, more powerful, MLP-like ANNs.
- ANNs more “chip-friendly” by definition: Mosaix chips, CNN here today, for embedded apps, massive thruput

# Neural Networks That Actually Work In Diagnostics, Prediction & Control: Common Misconceptions Vs. Real-World Success

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- Neural Nets, A Route to Learning/Intelligence
  - goals, history, basic concepts, consciousness
- State of the Art -- Working Tools Vs. Toys and Fads
  - static prediction/classification
  - dynamic prediction/classification
  - control: cloning experts, tracking, optimization
- Advanced Brain-Like Capabilities & Grids

# Neural Nets: The Link Between Vision, Consciousness and Practical Applications

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“Without **vision**, the people perish....”

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What is a Neural Network?

-- 4 **definitions**: “MatLab,” universal approximators,  
6<sup>th</sup> generation computing, brain-like computing

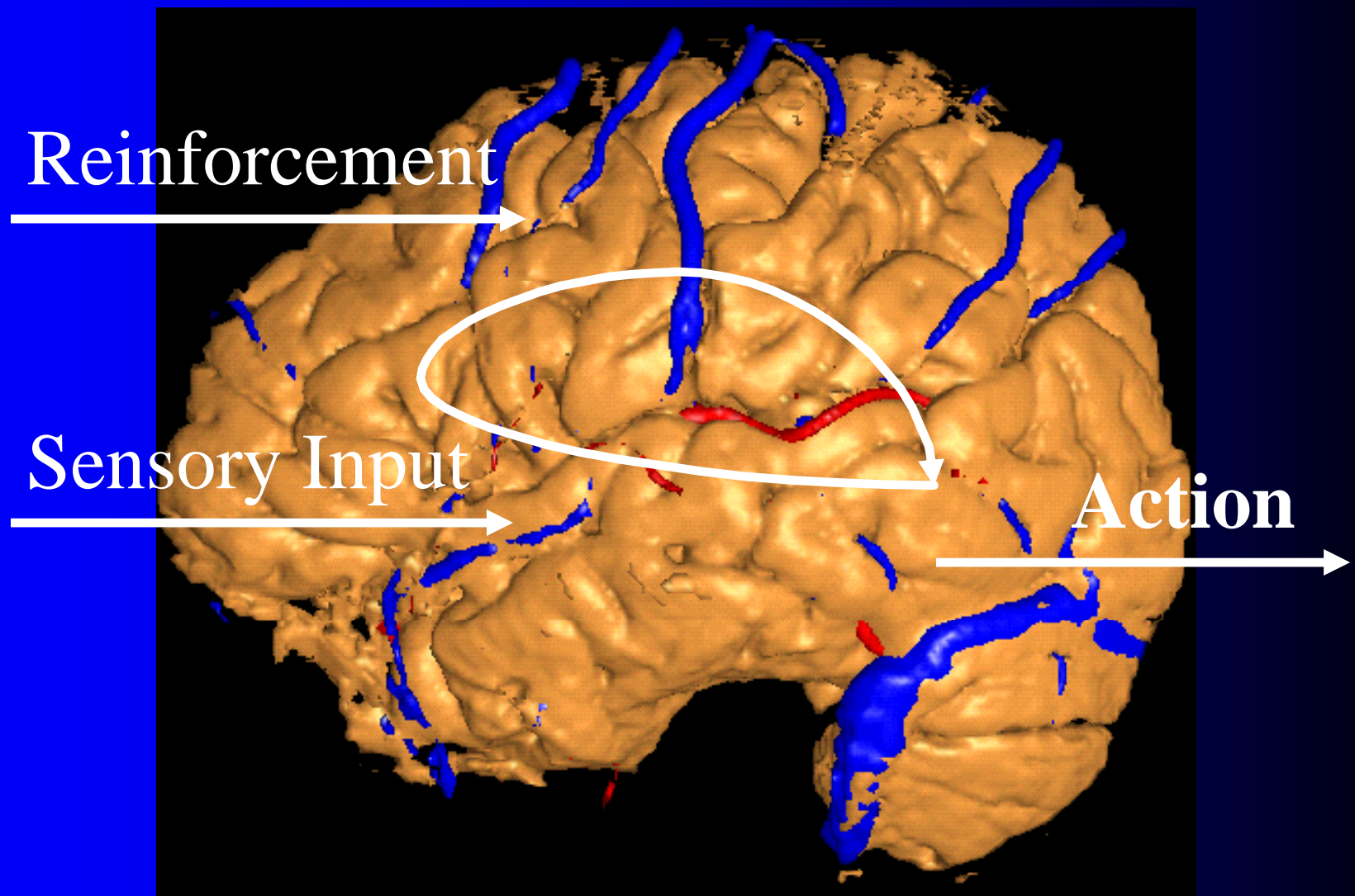
What is the Neural Network Field All About?

How Can We Get Better Results  
in Practical Applications?

# Generations of Computers

- ✧ 4th Gen: **Your PC**. One VLSI CPU chip executes one sequential stream of C code.
- ✧ 5th Gen: “MPP”, “**Supercomputers**”: Many CPU chips in 1 box. Each does 1 stream. HPCC.
- ✧ 6th Gen or “ZISC.” Ks or Millions of simple streams per chip or optics. **Neural nets** may be defined as designs for 6th gen + learning. (Psaltis, Mead.)
  - ✧ New interest; Moore, SRC; Mosaix, JPL sugarcube, CNN.
- ✧ 7th Gen: Massively parallel quantum computing?  
**General?** Grover like Hopfield?





**The Brain As a Whole System  
Is an Intelligent Controller**

# Unified Neural Network Designs:

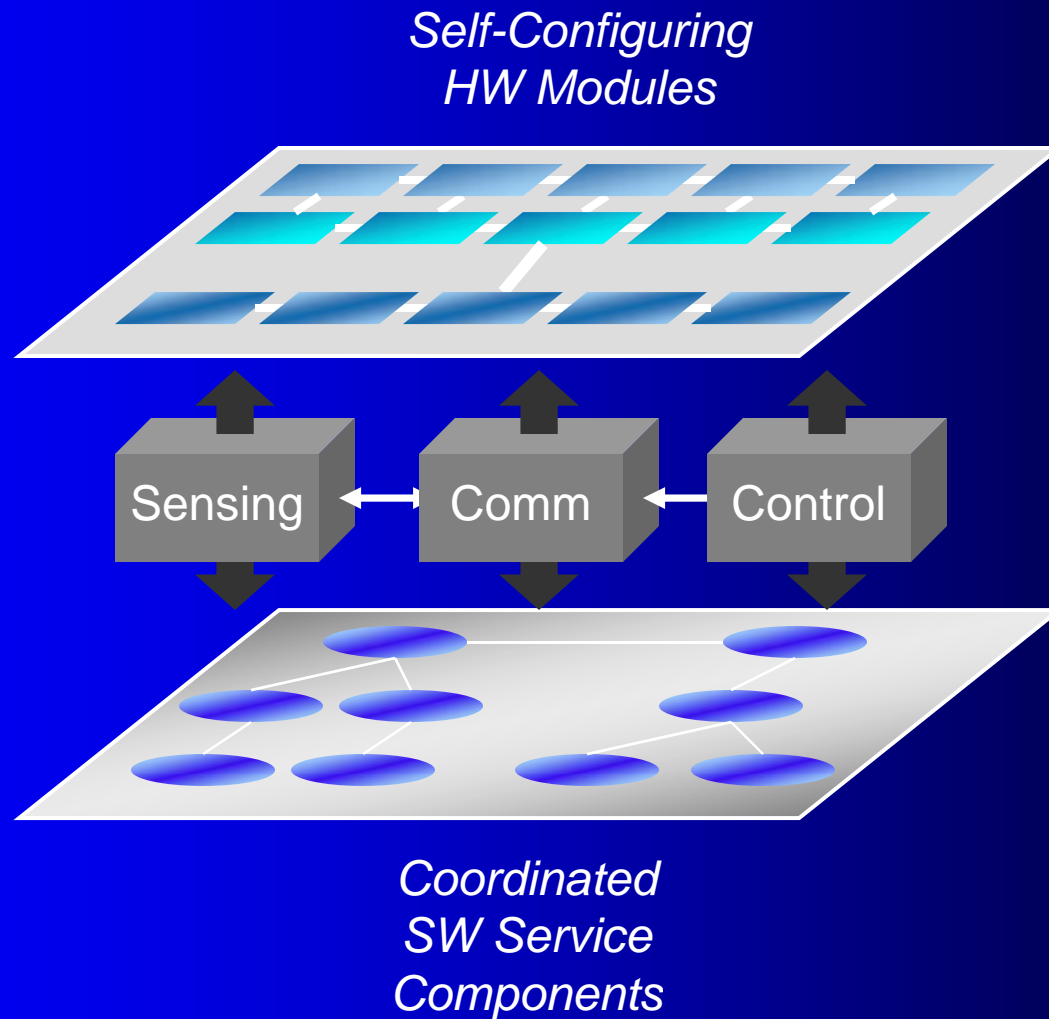
The Key to Large-Scale  
Applications  
& Understanding the Brain

# Electrical and Communications Systems(ECS) Cyber Infrastructure Investments

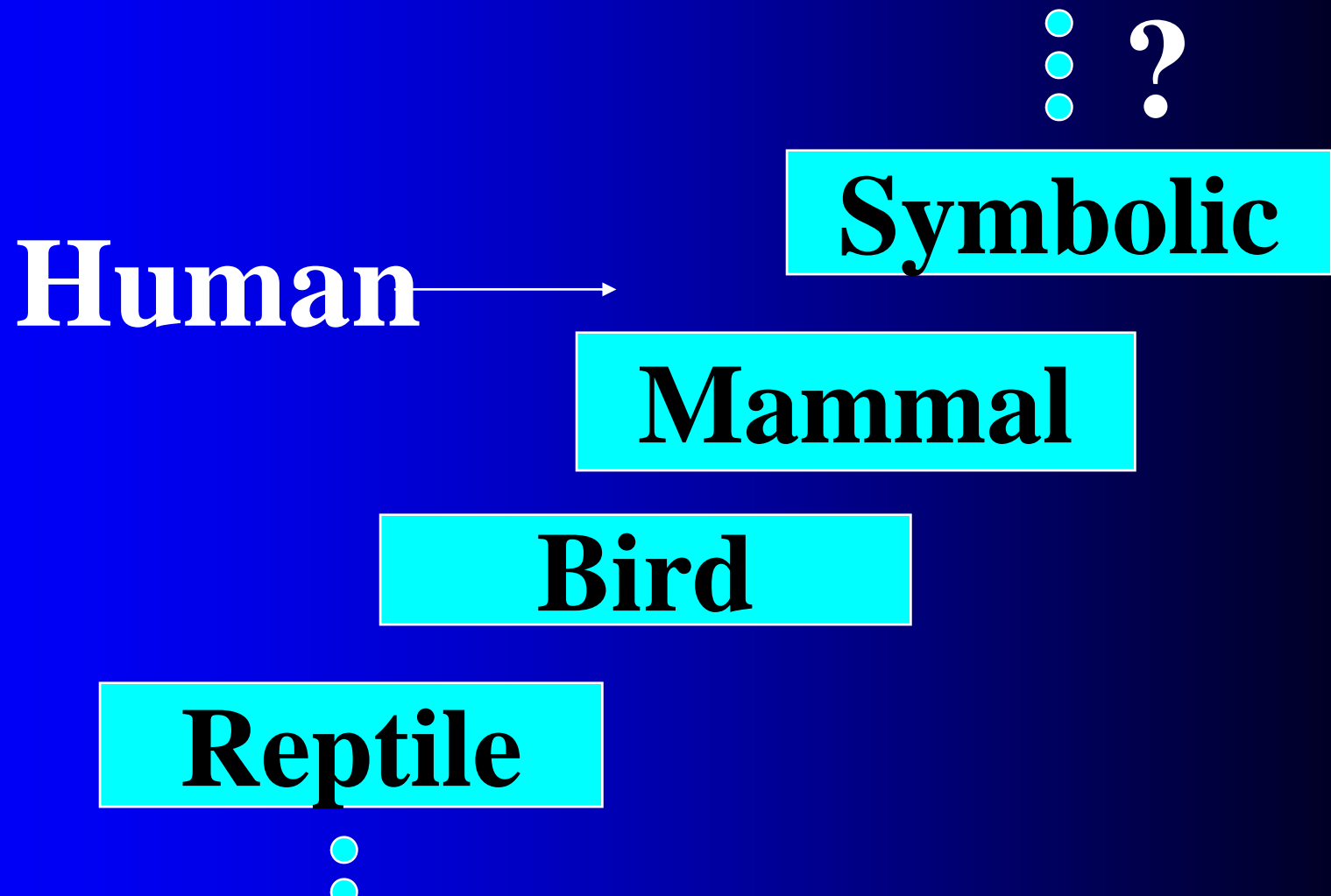
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- **The Physical Layer – Devices and Networks**
  - National Nanofabrication Users Network (NNUN)
  - Ultra-High-Capacity Optical Communications and Networking
  - Electric Power Sources, Distributed Generation and Grids
- **Information Layer – Algorithms, Information and Design**
  - **General** tools for distributed, robust, adaptive, hybrid control & related tools for modeling, system identification, estimation
  - **General** tools for sensors-to-information & to decision/control
  - Generality via computational intelligence, machine learning, neural networks & related pattern recognition, data mining etc.
- **Integration of Physical Layer and Information Layer**
  - Wireless Communication Systems
  - Self-Organizing Sensor and Actuator Networks
  - System on Chip for Information and Decision Systems
  - Reconfigurable Micro/Nano Sensor Arrays
  - Efficient and Secure Grids and Testbeds for Power Systems

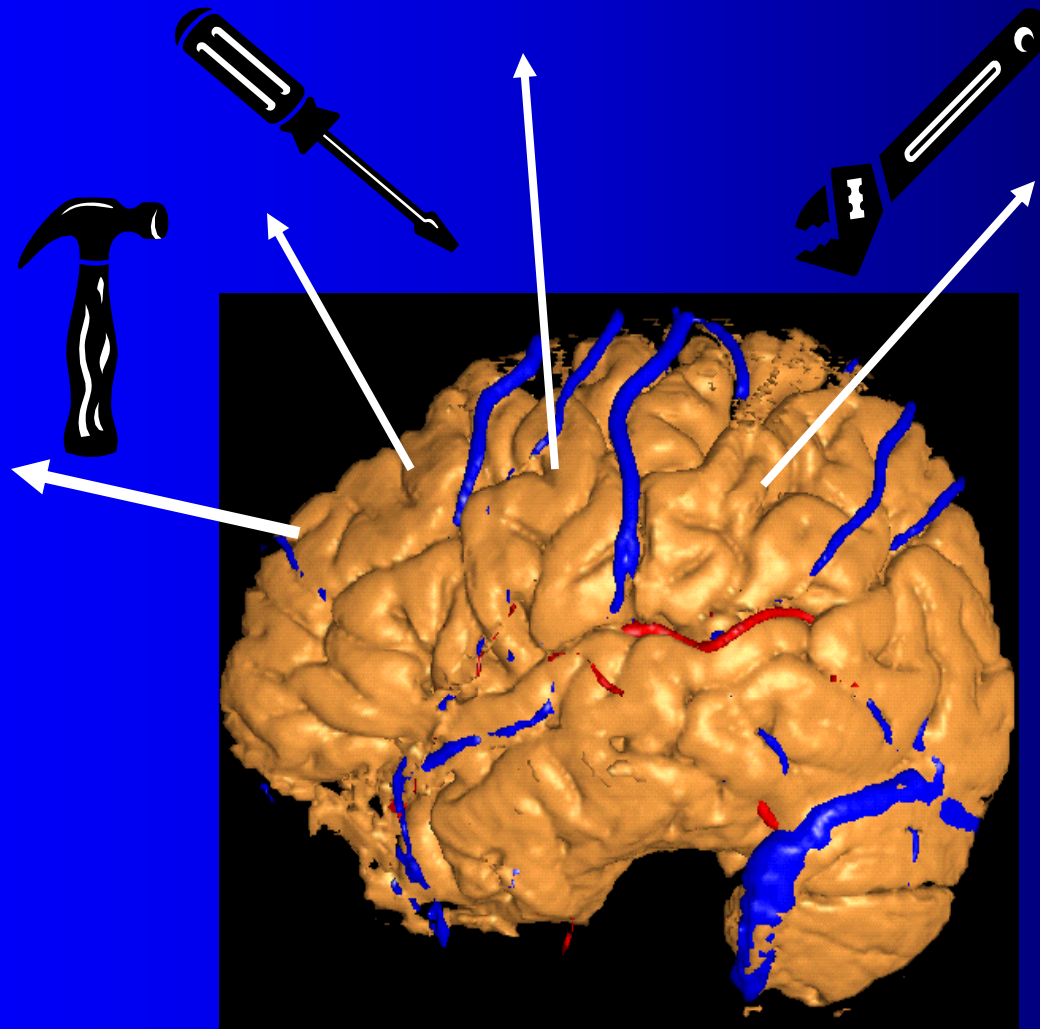
# Cyberinfrastructure: The Entire Web From Sensors To Decisions/Actions/Control For Max Performance



# Levels of Intelligence



# Why Engineers Need This **Vision**:



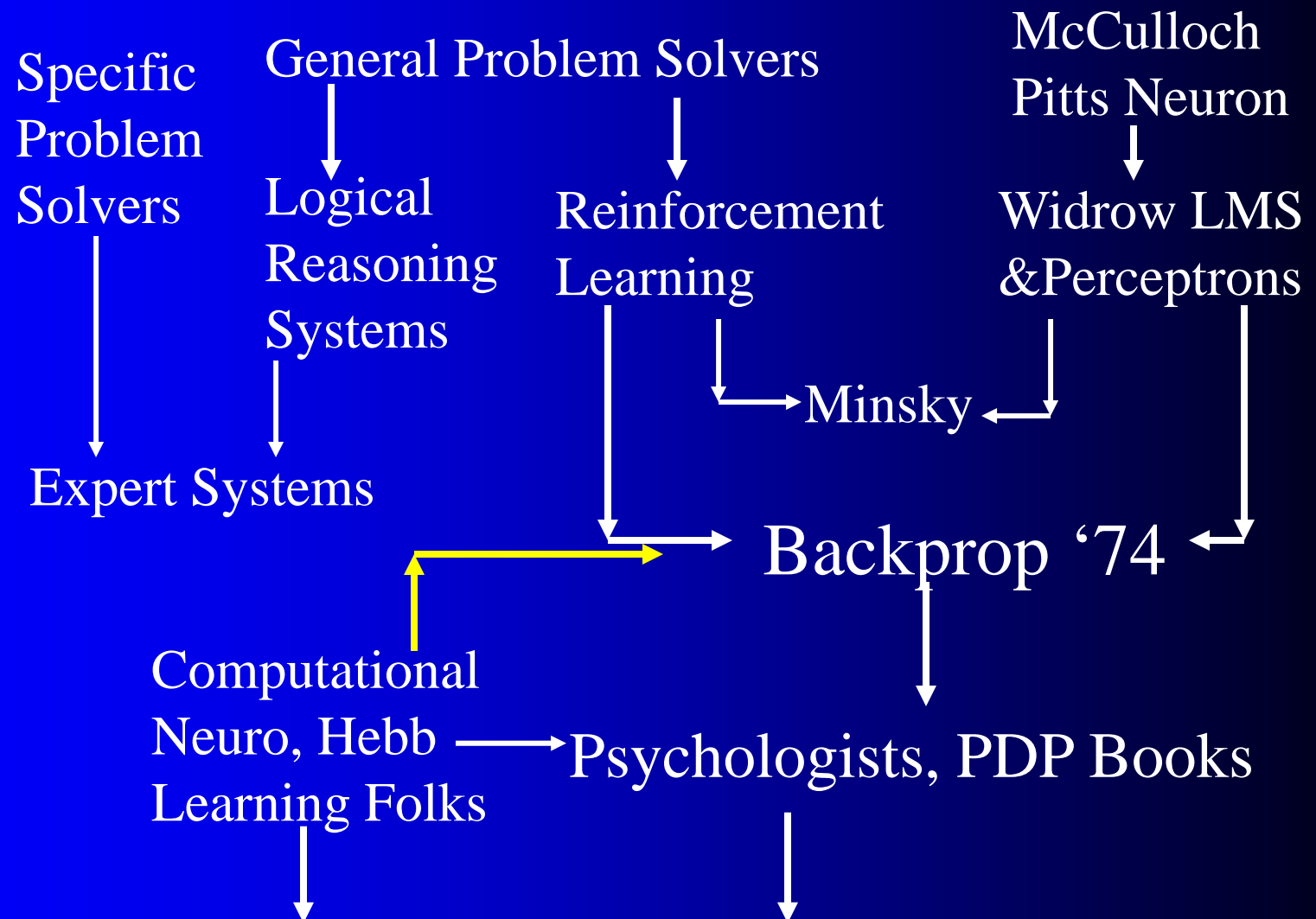
1. To Keep Track of **MANY** Tools

2. To Develop **New Tools** -- To Do Good R&D & Make Max Contribution

3. To Attract & Excite the **Best** Students

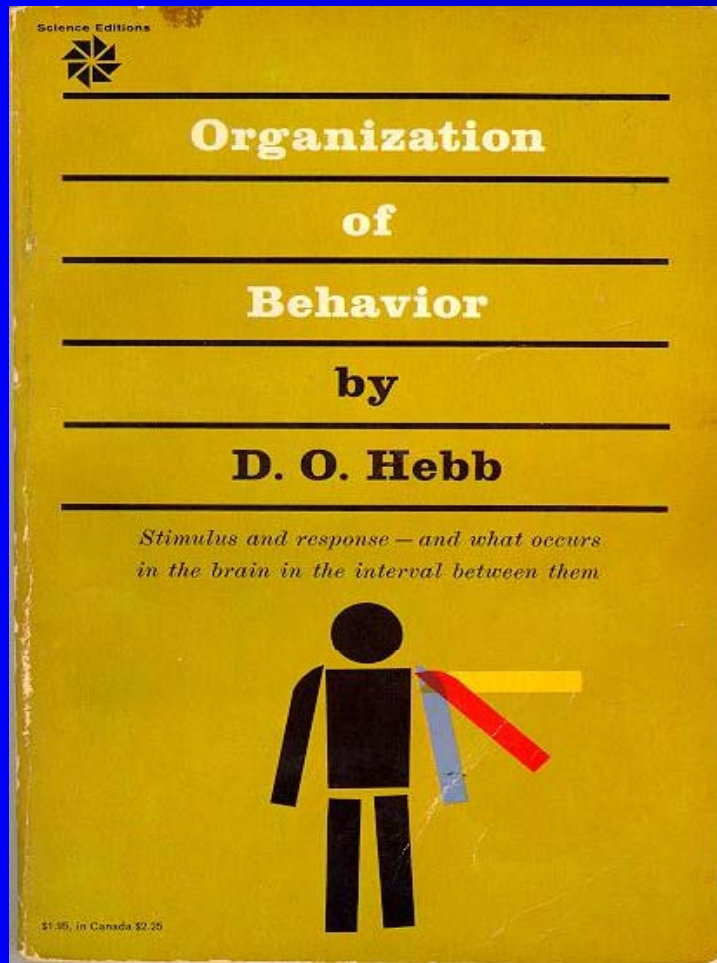
4. Engineers are Human Too...

# Where Did ANNs Come From?



IEEE ICNN 1987: Birth of a "Unified" Discipline

# Hebb 1949: Intelligence As An Emergent Phenomenon or Learning



“The general idea is an old one, that any two cells or systems of cells that are especially active at the same time will tend to become ‘associated,’ so that activity in one facilitates activity in the other” -- p.70 (Wiley 1961 printing)

The search for the General Neuron Model (of Learning)

“Solves all problems”



# Claim (1964) : Hebb's Approach Doesn't Quite Work As Stated

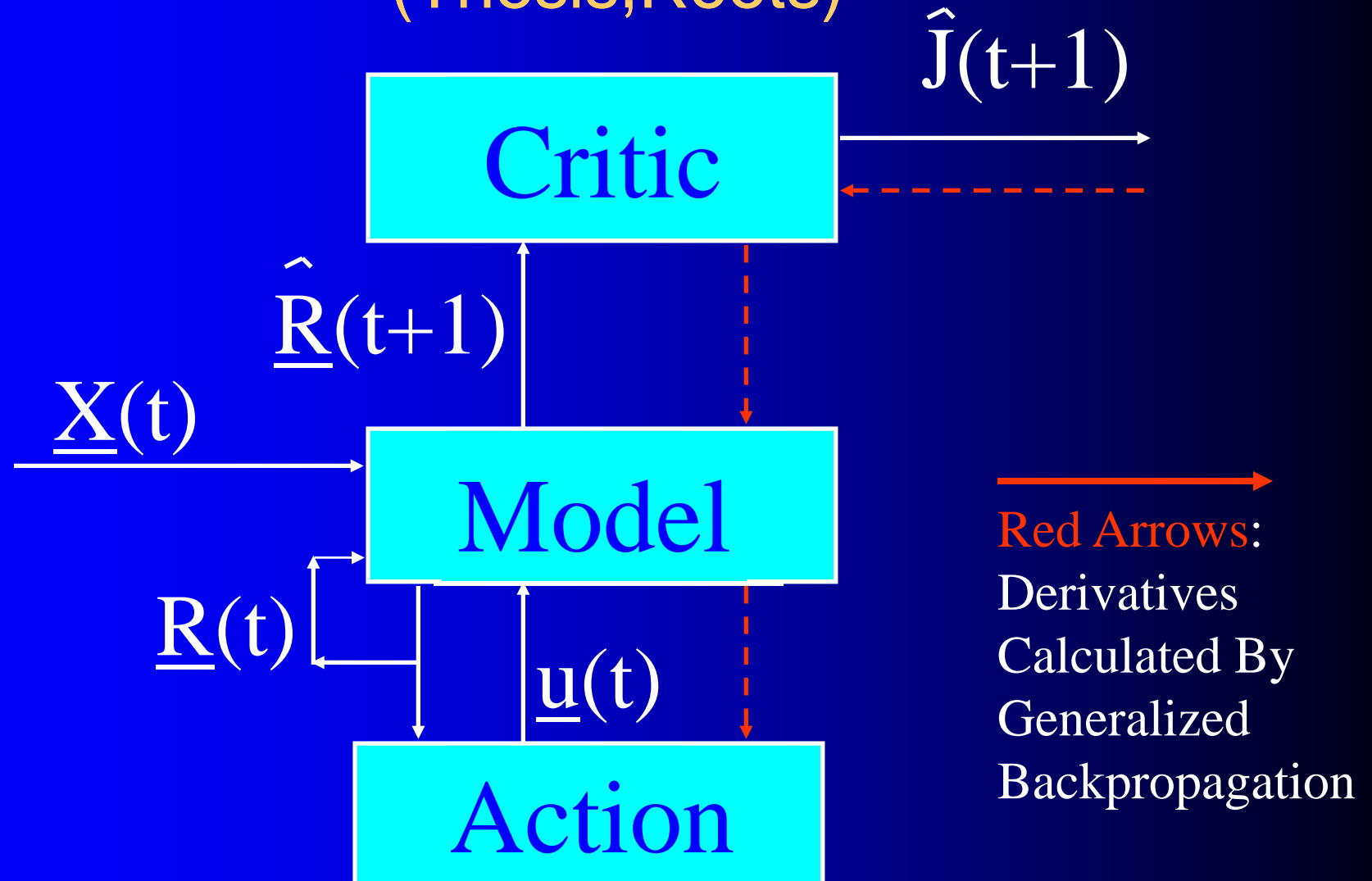
- Hebbian Learning Rules Are All Based on **Correlation Coefficients**
- Good Associative Memory: **one component** of the larger brain (Kohonen, ART, Hassoun)
- **Linear** decorrelators and predictors
- Hopfield  $f(\underline{u})$  minimizers never scaled, **but**:
  - Gursel Serpen and SRN minimizers
  - Brain-Like Stochastic Search (Needs R&D)

# Understanding Brain Requires Models Tested/Developed Using Multiple Sources of Info

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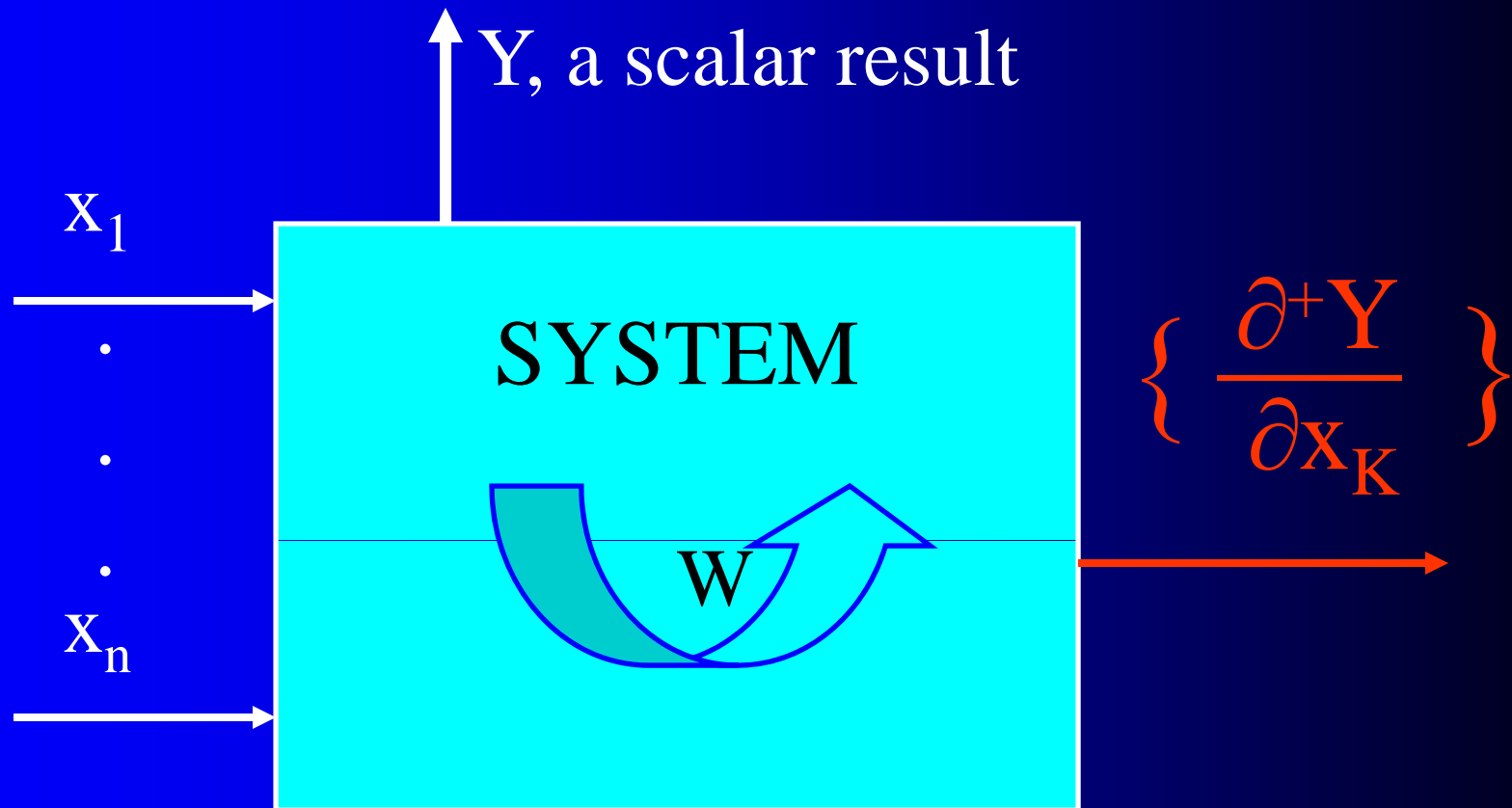
- Engineering: Will it work? Mathematics understandable, generic?
- Psychology: Connectionist cognitive science, animal learning, folk psychology
- Neuroscience: computational neuroscience
- AI: agents, games (backgammon, go), etc.
- LIS and CRI

# 1971-2: Emergent Intelligence Is Possible If We Allow Three Types of Neuron (Thesis, Roots)



# Harvard Committee Response

- We don't believe in neural networks – see Minsky (Anderson&Rosenfeld, Talking Nets)
- **Prove** that your backwards differentiation works. (That is enough for a PhD thesis.) The critic/DP stuff published in '77,'79,'81,'87..
- **Applied** to affordable vector ARMA statistical estimation, general TSP package, and robust political forecasting

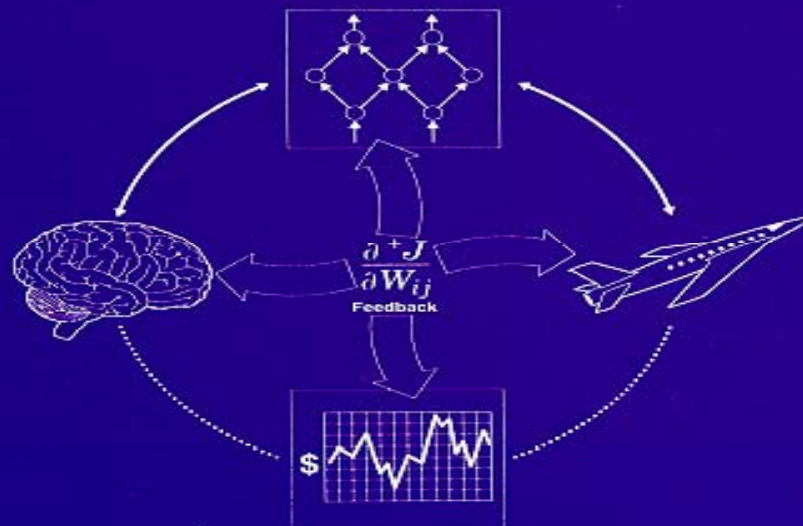


(Inputs  $x_k$  may actually come from many times)

**Backwards Differentiation:** But what kinds of SYSTEM can we handle? See details in AD2004 Proceedings, Springer, in press.

# THE ROOTS OF BACKPROPAGATION

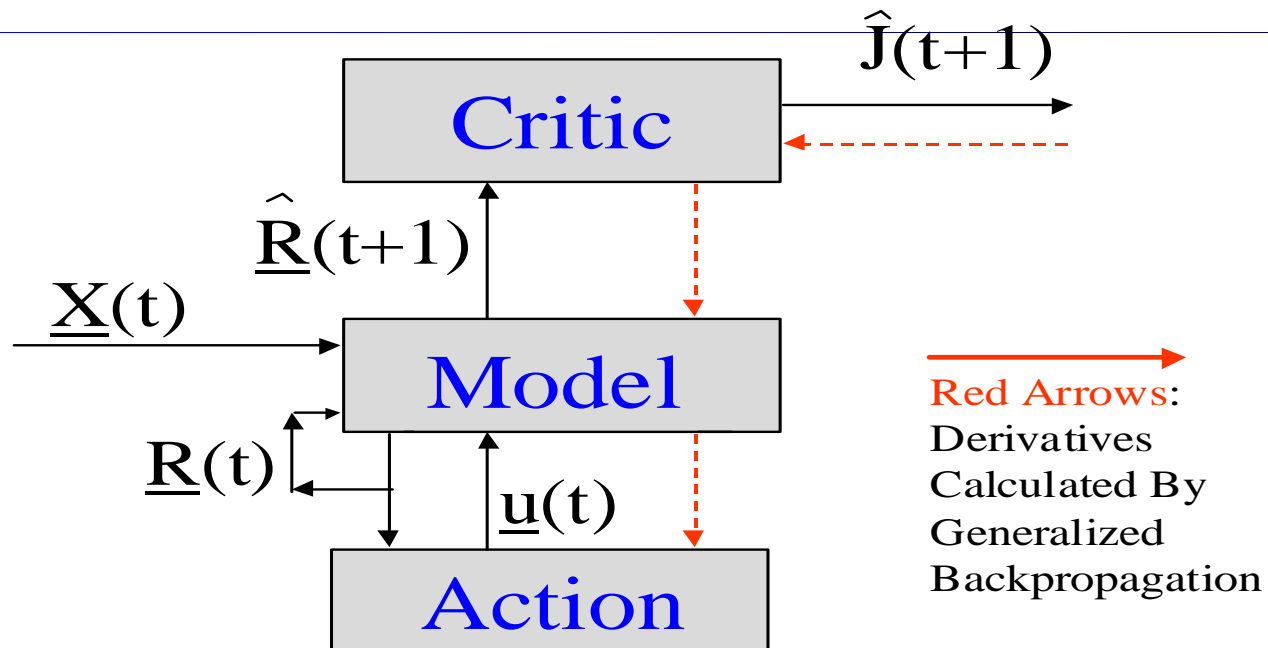
From Ordered Derivatives  
to Neural Networks  
and Political Forecasting



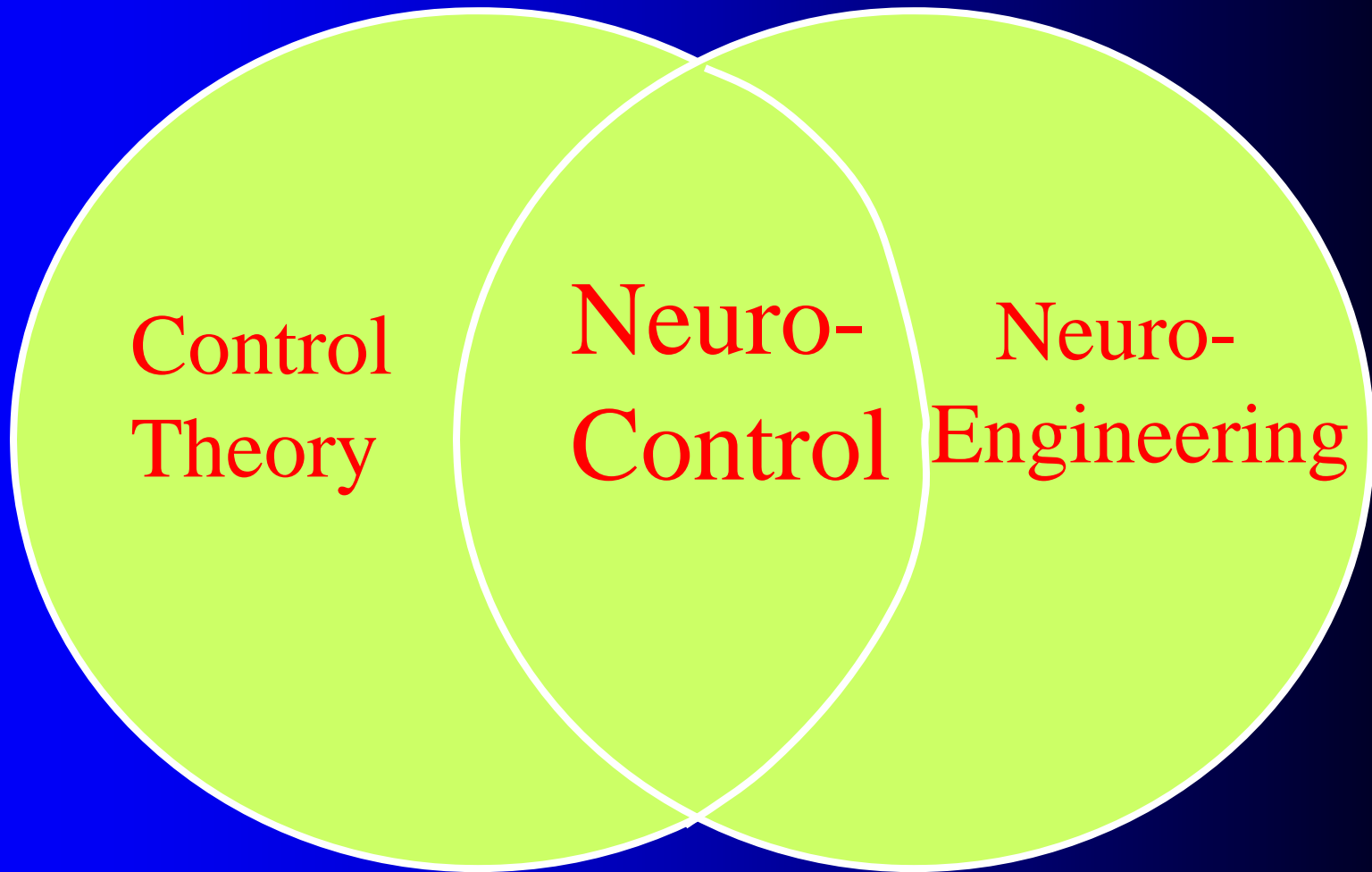
**PAUL JOHN WERBOS**

A Volume in the Wiley Series on ADAPTIVE AND LEARNING SYSTEMS  
FOR SIGNAL PROCESSING, COMMUNICATIONS, AND CONTROL  
SIMON HAYKIN, SERIES EDITOR

- To Fill IN the Boxes:
- (1) NEUROCONTROL, to Fill in Critic or Action;
  - (2) System Identification or Prediction (Neuroidentification) to Fill In Model



# NSF Workshop Neurocontrol 1988

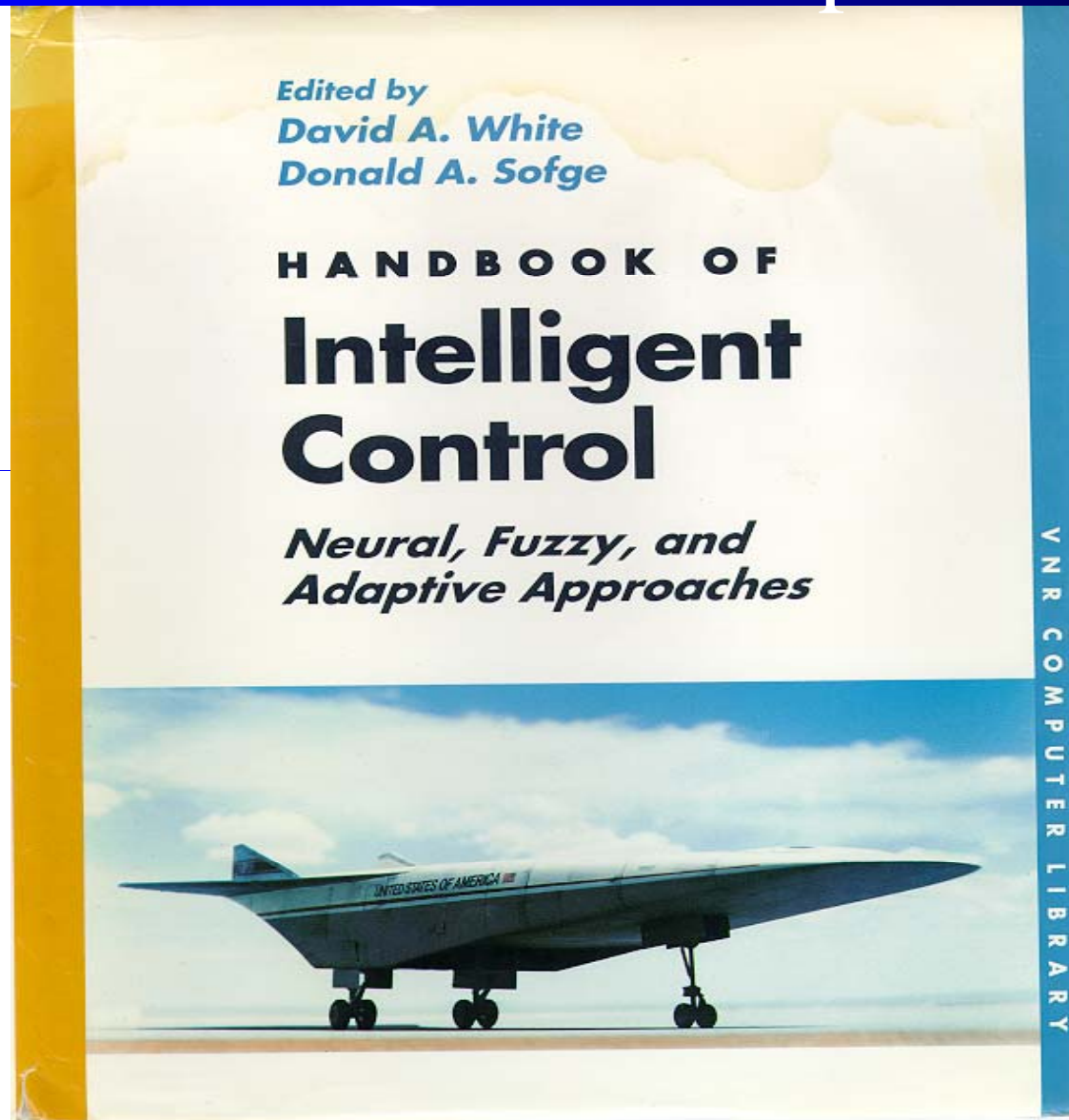


Miller, Sutton, Werbos, MIT Press, 1990

**Neurocontrol is NOT JUST Control Theory!**



# NSF/McAir Workshop 1990



White and Sofge eds, Van Nostrand, 1992

“What Do Neural Nets &  
Quantum  
Theory Tell Us About Mind &  
Reality?”

In Yasue et al (eds),  
*No Matter, Never Mind -- Proc.  
Of Towards a Science of  
Consciousness*, John Benjamins  
(Amsterdam), 2001 & arxiv.org

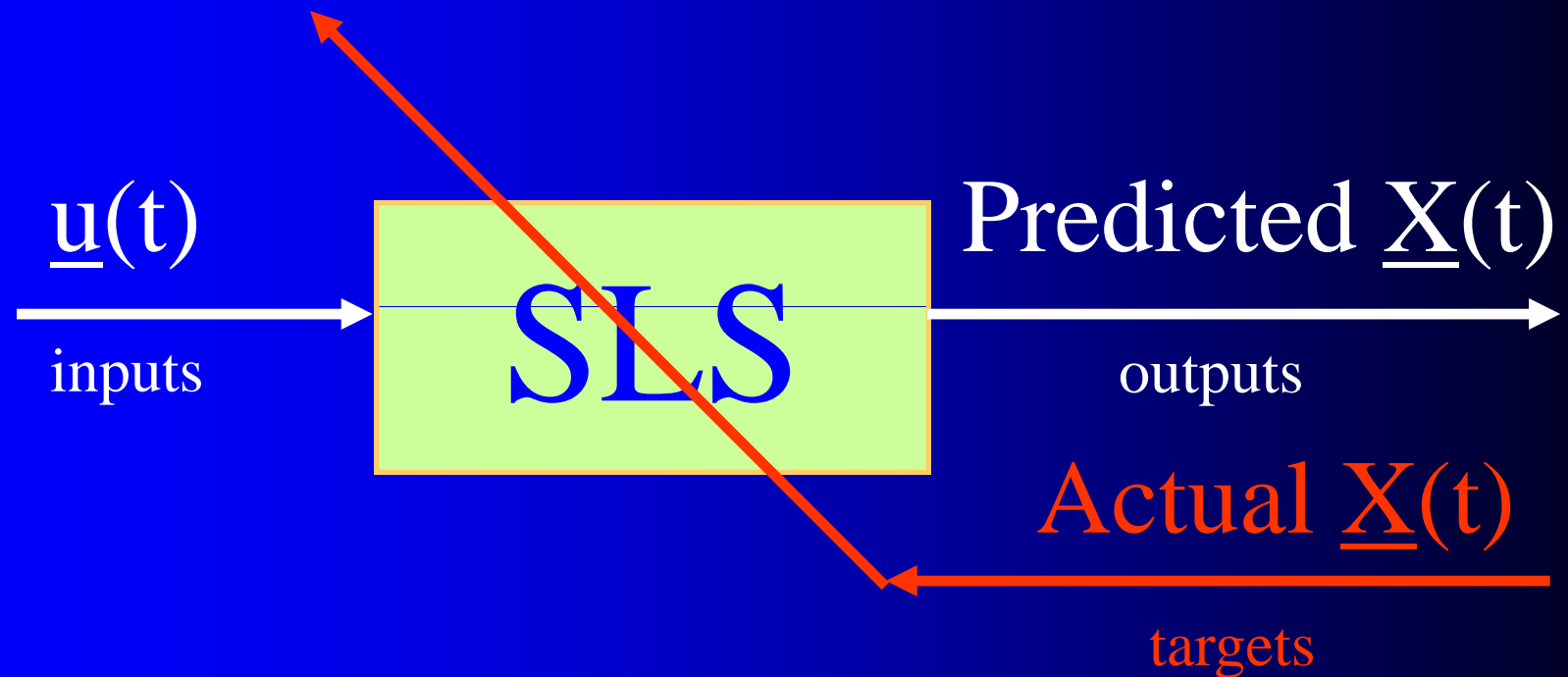
# 3 Types of Diagnostic System

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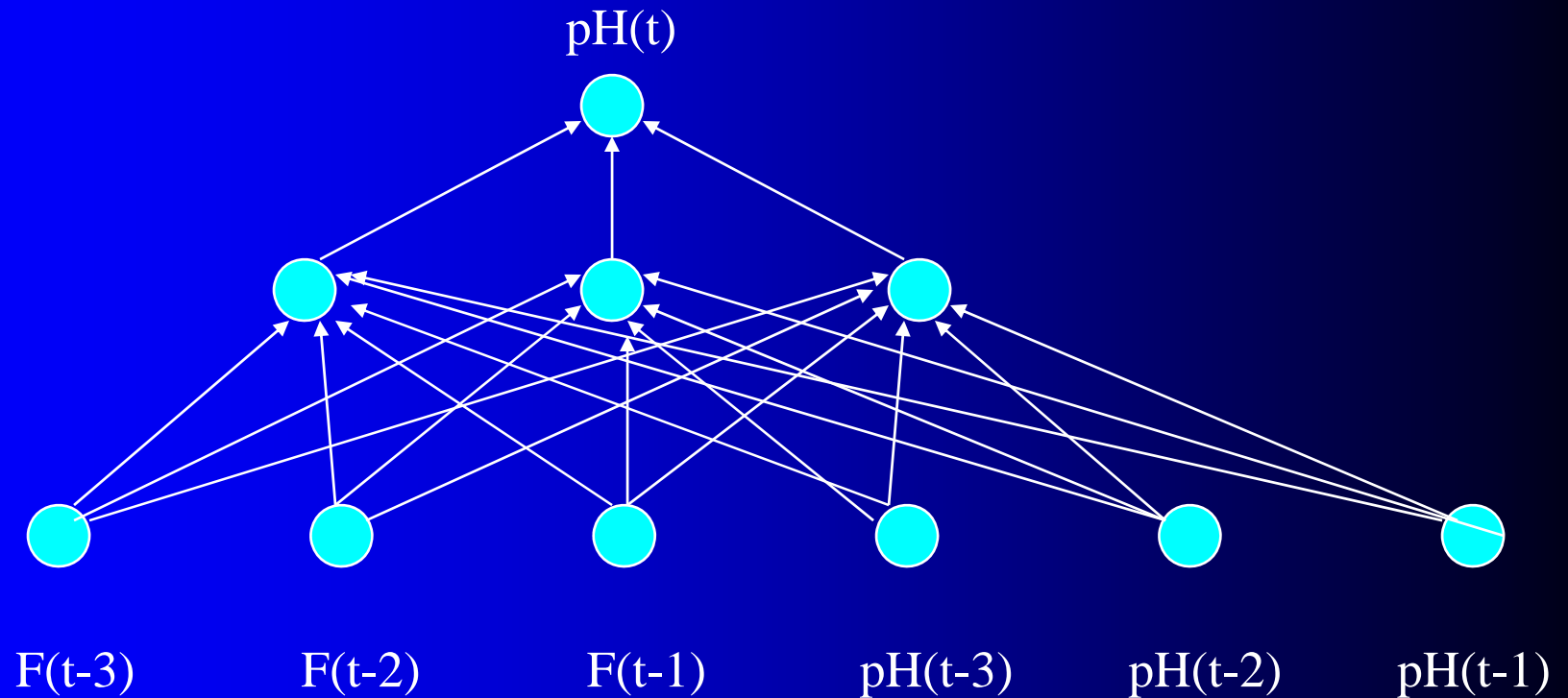
- All 3 train **predictors**, use sensor data  $\underline{X}(t)$ , other data  $\underline{u}(t)$ , fault classifications  $F_1$  to  $F_m$
- Type 1: predict  $F_i(t)$  from  $\underline{X}(t)$ ,  $\underline{u}(t)$ , MEMORY
- Others: first train to predict  $\underline{X}(t+1)$  from  $\underline{X}, \underline{u}, \text{MEM}$ 
  - Type 2: when **actual**  $\underline{X}(t+1)$   $6\sigma$  from prediction, ALARM
  - Type 3: if prediction net **predicts BAD**  $\underline{X}(t+T)$ , ALARM
- Combination best. See PJW in Maren, ed, *Handbook Neural Computing Apps*, Academic, 1990.

# Supervised Learning Systems (SLS)

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SLS may have internal dynamics but no “memory” of times  $t-1$ ,  $t-2$ ...



Example of TDNN used in HIC, Chapter 10

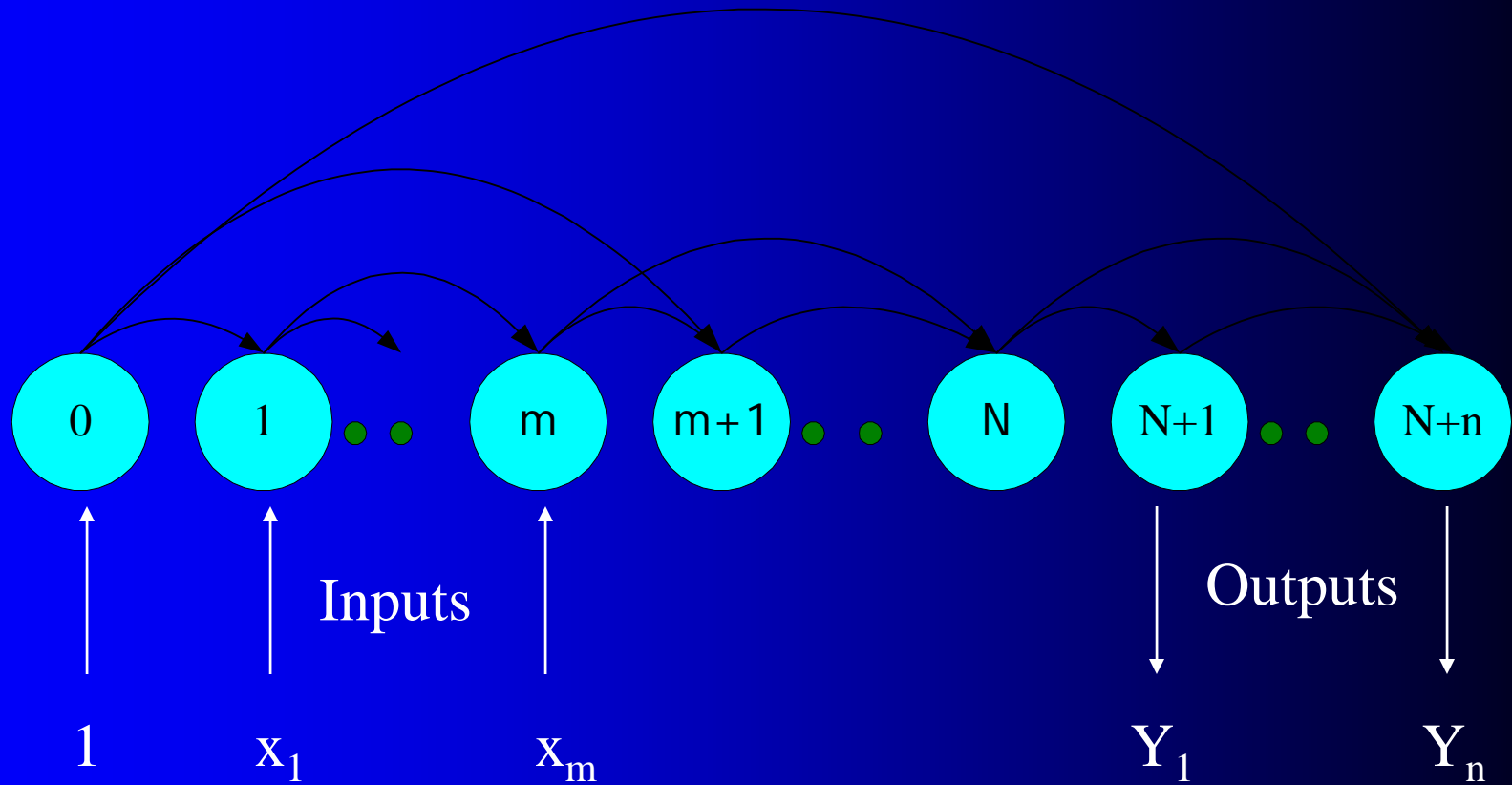
TDNNs learn NARX or FIR Models, not NARMAX or IIR

# CONVENTIONAL ANNS USED FOR FUNCTION APPROXIMATION IN CONTROL

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- Global: Multilayer Perceptron (MLP)
  - Better Generalization, Slower Learning
  - Barron's Theorems: More Accurate Approximation of Smooth Functions as Number of Inputs Grows
- Local: RBF, CMAC, Hebbian
  - Like Nearest Neighbor, Associative Memory
  - Sometimes Called "Glorified Lookup tables"

# Generalized MLP



# No feedforward or associative memory net can give brain-like performance! Useful recurrence--

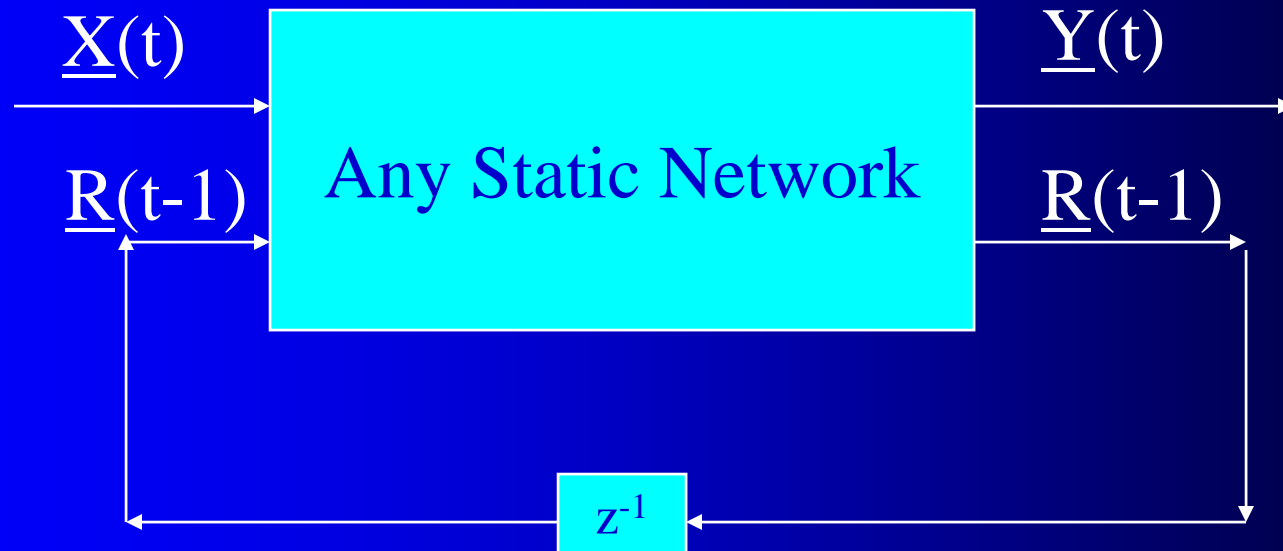
- For short-term memory, for state estimation, for fast adaptation – **time-lagged recurrence** needed. (**TLRN** – time-lagged recurrent net)
- For better  $Y=F(X,W)$  mapping, **Simultaneous Recurrent Networks** Needed. For large-scale tasks, **SRNs WITH SYMMETRY** tricks needed – cellular SRN, Object Nets
- For robustness over time, “recurrent training”



# Why TLRNs Vital in Prediction: Correlation $\neq$ Causality!

- E.g.: law X sends extra \$ to schools with low test scores
- Does negative correlation of \$ with test scores imply X is a bad program? No! Under such a law, negative correlation is hard-wired. Low test scores cause \$ to be there! No evidence + or - re the program effect!
- Solution: compare \$ at time t with performance changes from t to t+1! More generally/accurately: train dynamic model/network – essential to any useful information about causation or for decision!

# The Time-Lagged Recurrent Network (TLRN)



$$\underline{Y}(t) = \underline{f}(\underline{X}(t), \underline{R}(t-1)); \underline{R}(t) = \underline{g}(\underline{X}(t), \underline{R}(t-1))$$

$\underline{f}$  and  $\underline{g}$  represent 2 outputs of one network

All-encompassing, NARMAX(1  $\equiv$  n)

Felkamp/Prokhorov Yale03:  $\gg$ EKF,  $\approx$  hairy

# 4(5) Ways to Train TLRNs (SRN)

(arXiv.org, adap-org 9806001)

- “Simple BP” – incorrect derivatives due to truncated calculation, robustness problem
- BTT – exact, efficient, see Roots of BP ('74), but not brain-like (back time calculations)
- Forward propagation – many kinds (e.g, Roots, ch.7, 1981) – not brainlike,  $O(nm)$
- **Error Critic** – see Handbook ch. 13, Prokhorov
- **Simultaneous BP** – SRNS only.

# 4 Training Problems Recurrent Nets

- Bugs – need good diagnostics
- “Bumpy error surface” – Schmidhuber says is common, Ford not. Sticky neuron, RPROP, DEFK (Ford), etc.
- Shallow plateaus – adaptive learning rate, DEKF etc., new in works...
- Local minima – shaping, unavoidable issues, creativity

# GENERALIZED MAZE PROBLEM

$J_{\text{hat}}(ix, iy)$  for all  $0 < ix, iy < N+1$   
(an  $N$  by  $N$  array)

**NETWORK**

Maze Description

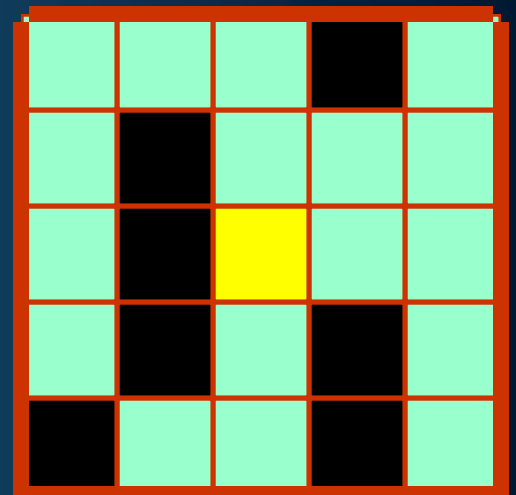
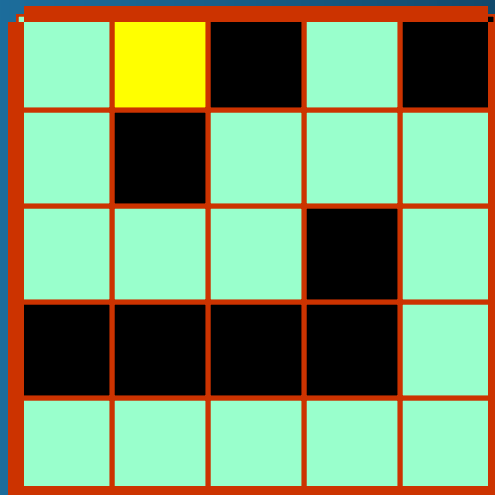
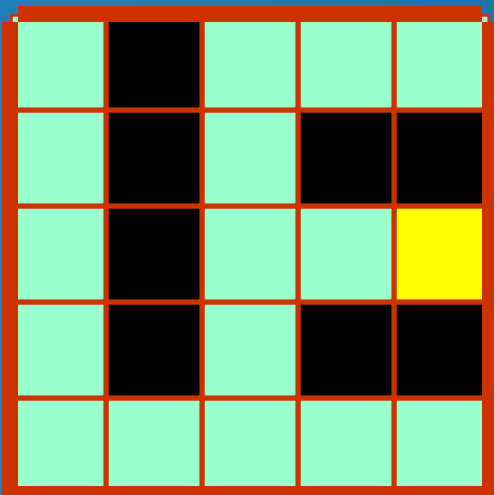
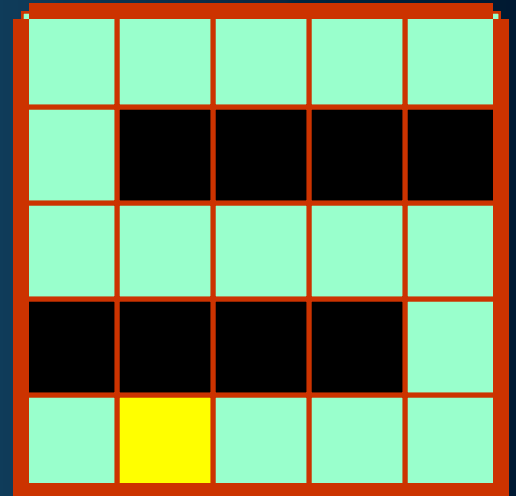
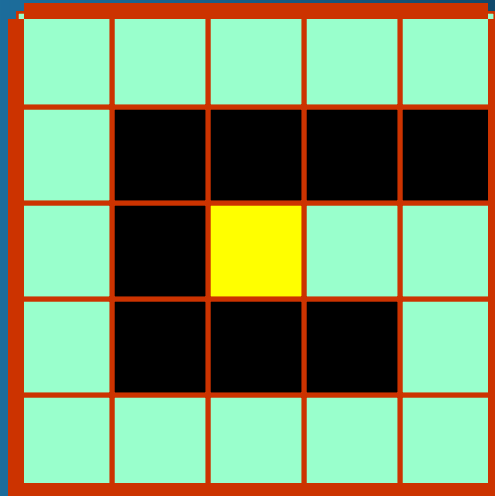
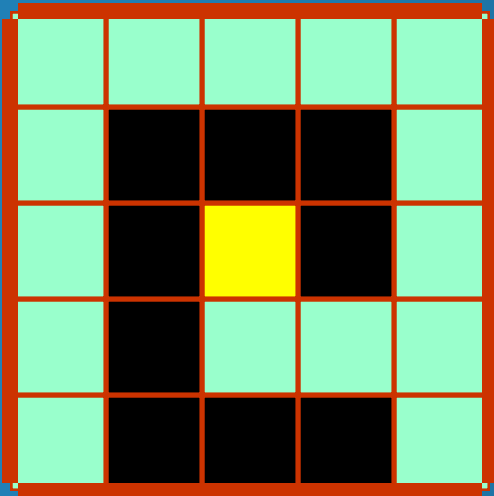
- Obstacle  $(ix, iy)$  all  $ix, iy$
- Goal  $(ix, iy)$  all  $ix, iy$

At [arXiv.org](http://arXiv.org), [nlin-sys](http://nlin-sys), see [adap-org](http://adap-org) 9806001

4	3	2	1	2
5		1	0	1
6	7		1	2
7	8	7		3
8	7	6	5	4

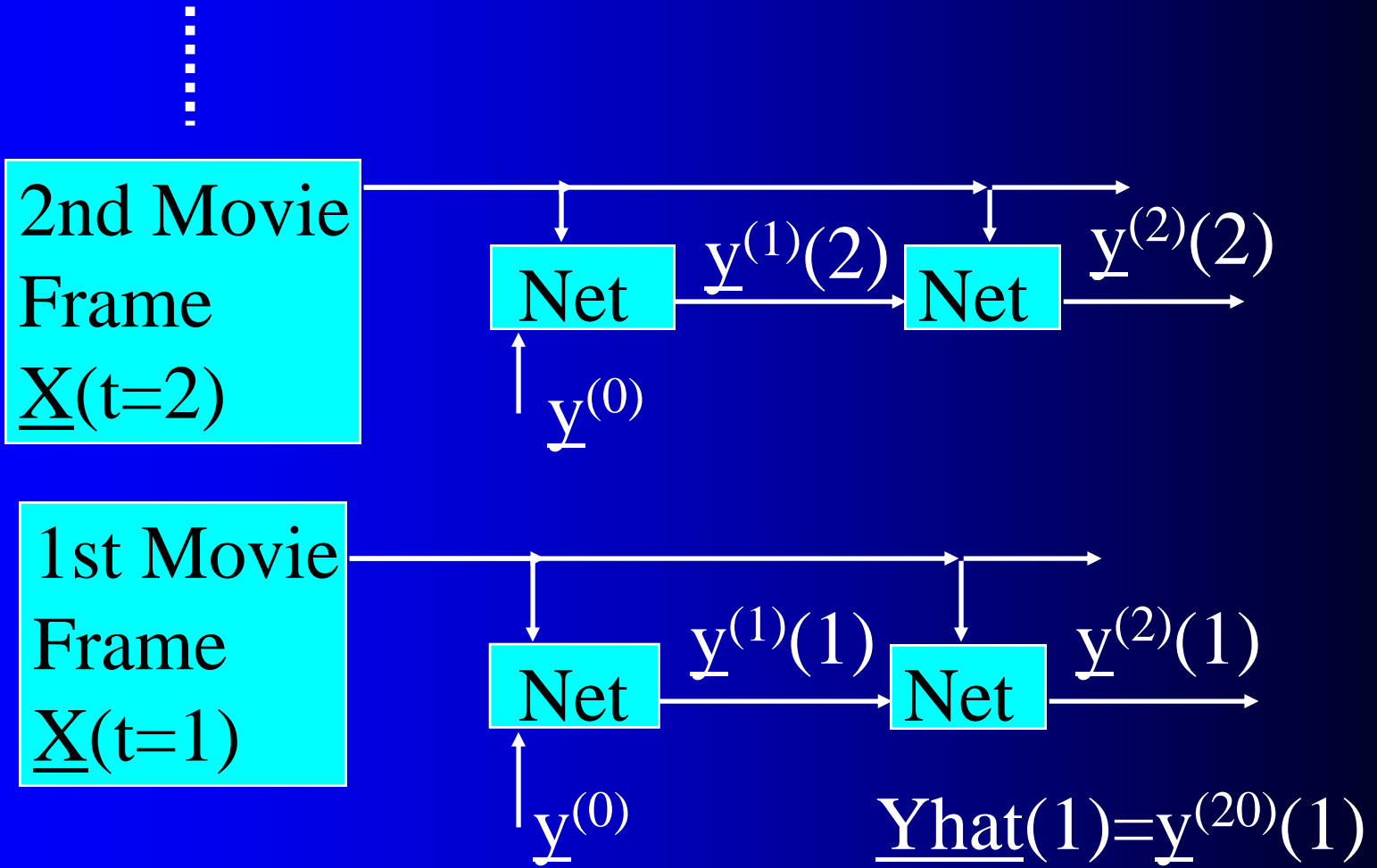




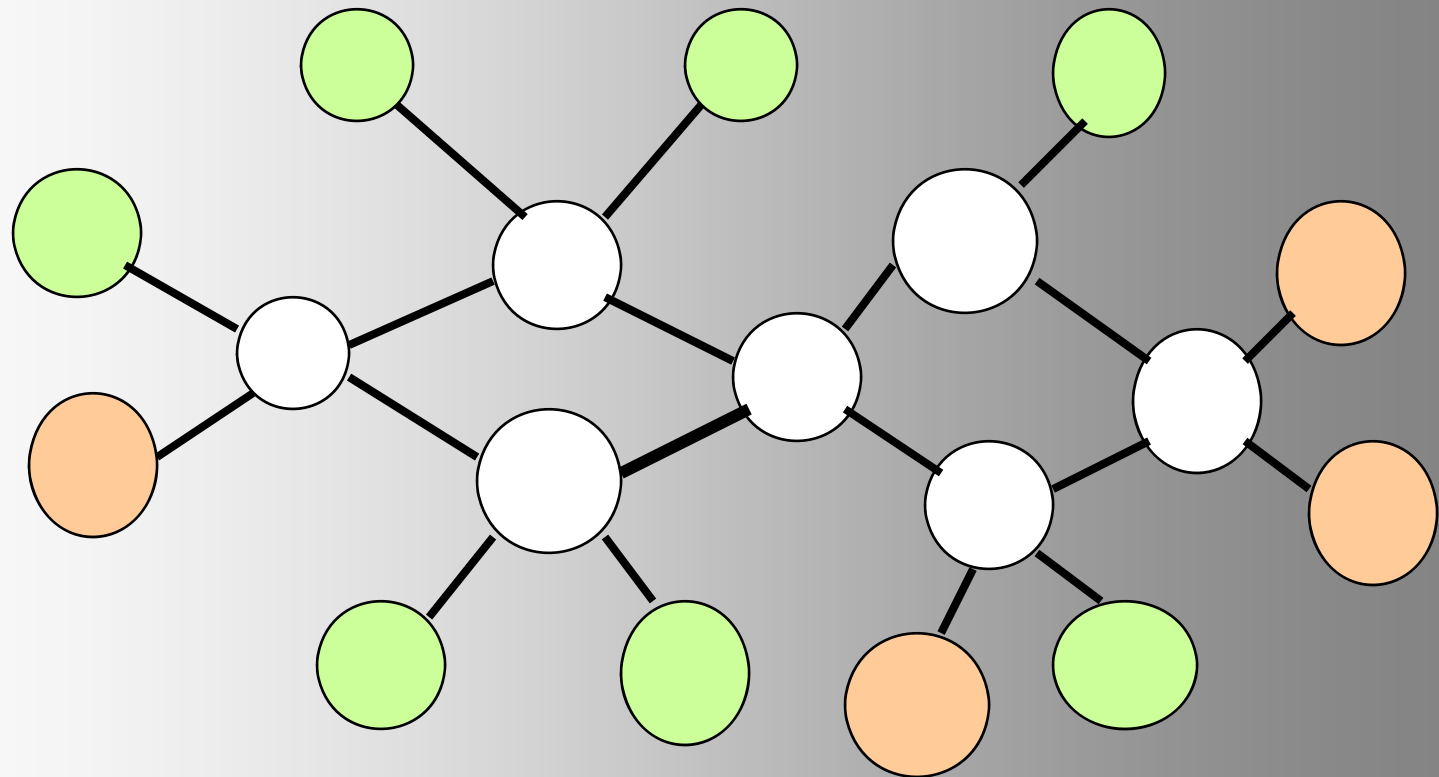
# IDEA OF SRN: TWO TIME INDICES $t$ vs.

$n$





# ANN to I/O From Idealized Power Grid



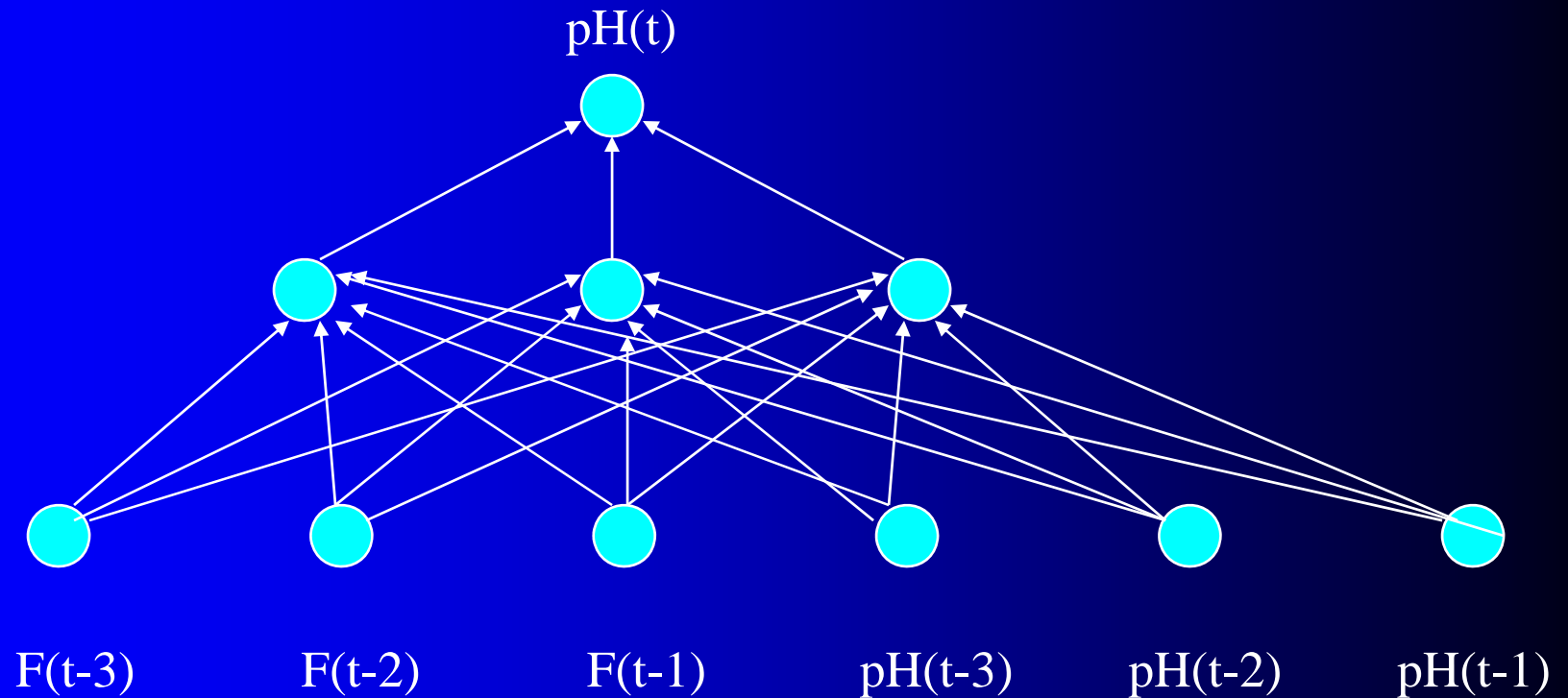
- 4 General Object Types (busbar, wire, G, L)
- Net should allow **arbitrary number** of the 4 objects
- How design ANN to input and output FIELDS -- variables like the SET of values for current ACROSS all objects?

# Training: Brain-Style Prediction Is NOT Just Time-Series Statistics!

- One System **does it all** -- not just a collection of chapters or methods
- Domain-specific info is 2-edged sword:
  - need to use it; **need to be able to do without it**
- Neural Nets demand/inspire new work on **general-purpose prior probabilities** and on **dynamic robustness** (See HIC chapter 10)
- SEDP&Kohonen: general nonlinear **stochastic ID** of partially observed systems

# Three Approaches to Prediction

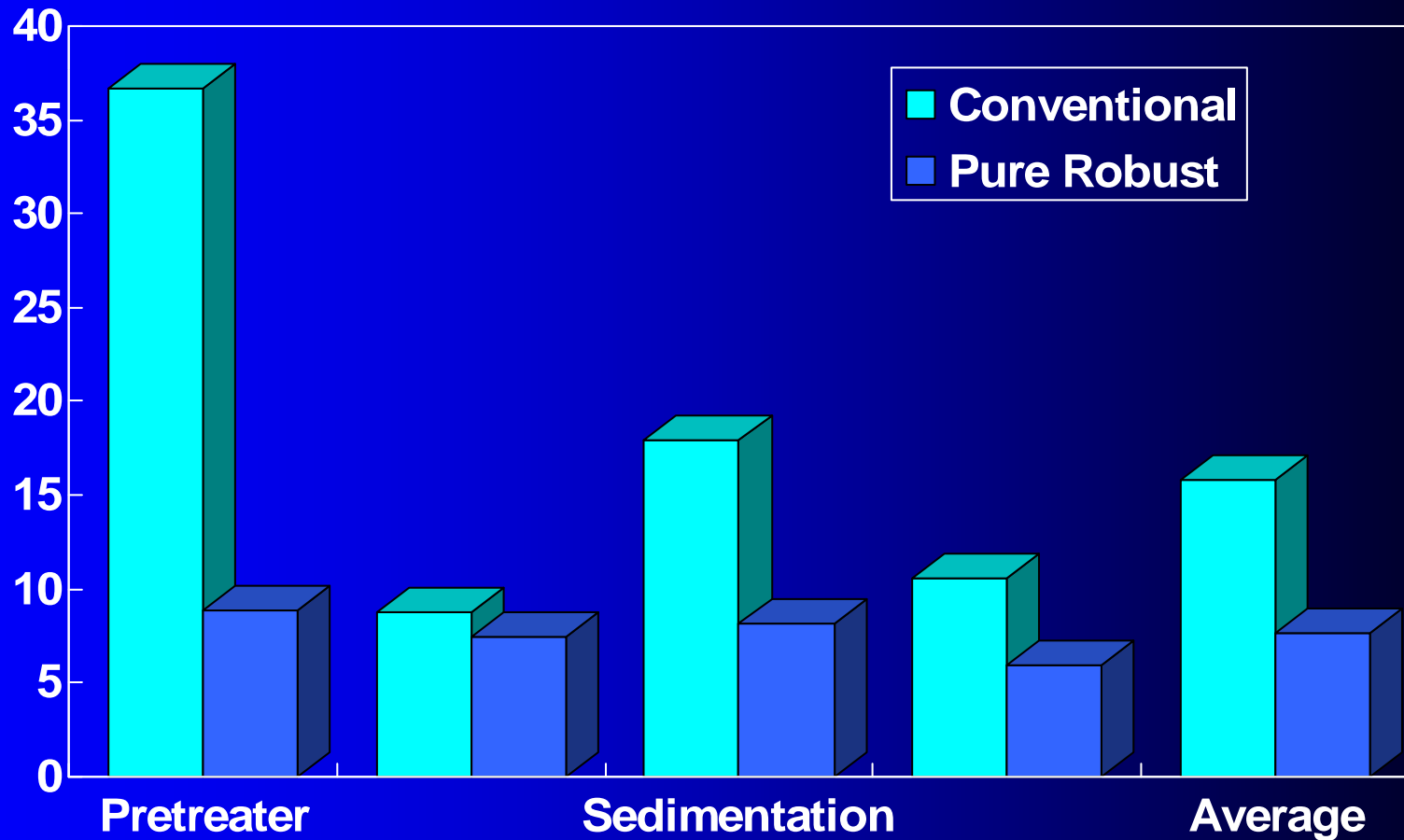
- Bayesian: Maximize  $\Pr(\text{Model}|\text{data})$ 
  - “Prior probabilities” essential when many inputs
- Minimize “bottom line” directly
  - Vapnik: “empirical risk” static SVM and “structural risk” error bars around same like linear robust control on nonlinear system
  - Werbos ’74 thesis: “pure robust” time-series
- Reality: Combine understanding and bottom line.
  - Compromise method (Handbook)
  - Model-based adaptive critics
- Suykens, Land????



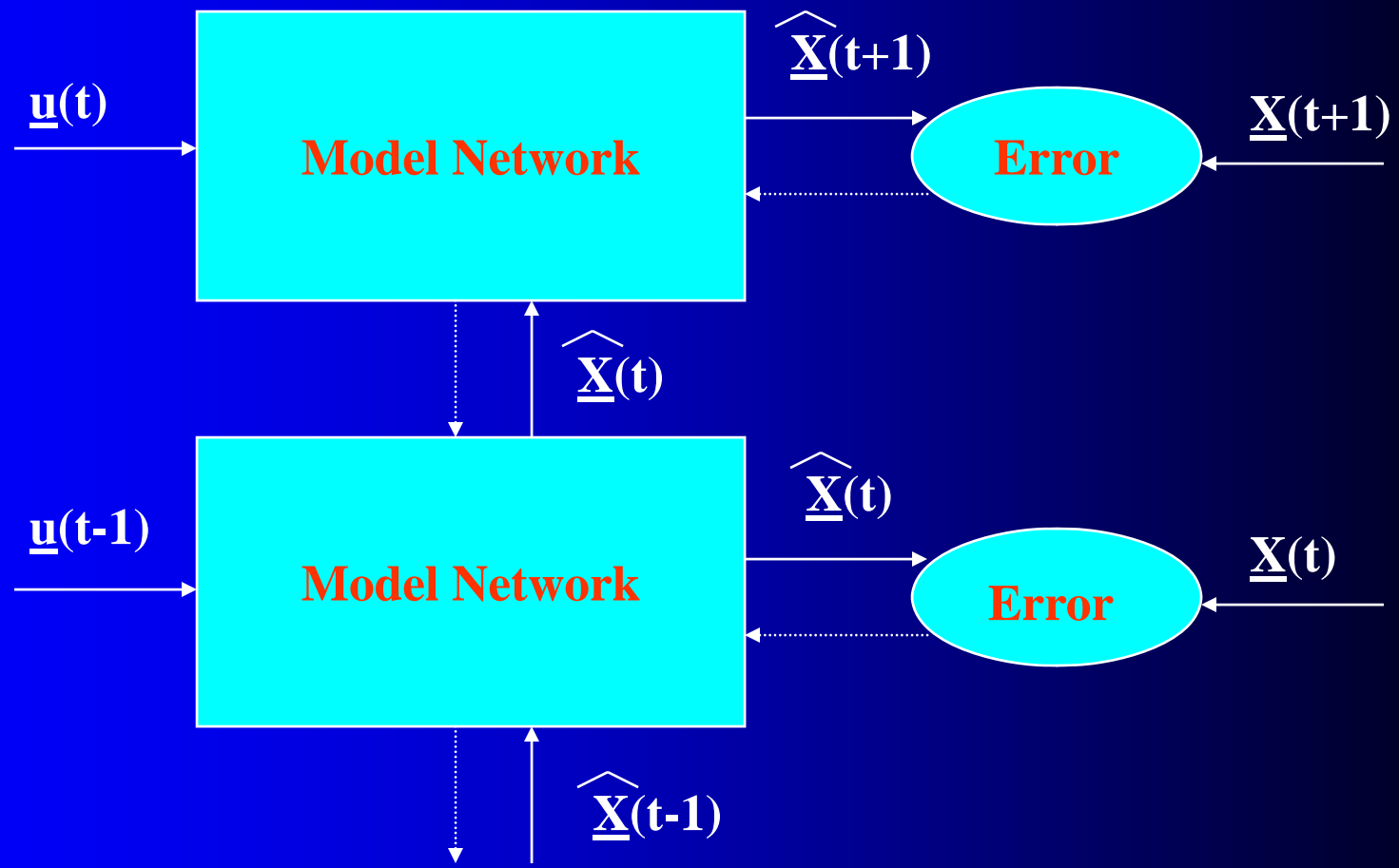
Example of TDNN used in HIC, Chapter 10

TDNNs learn NARX or FIR Models, not NARMAX or IIR

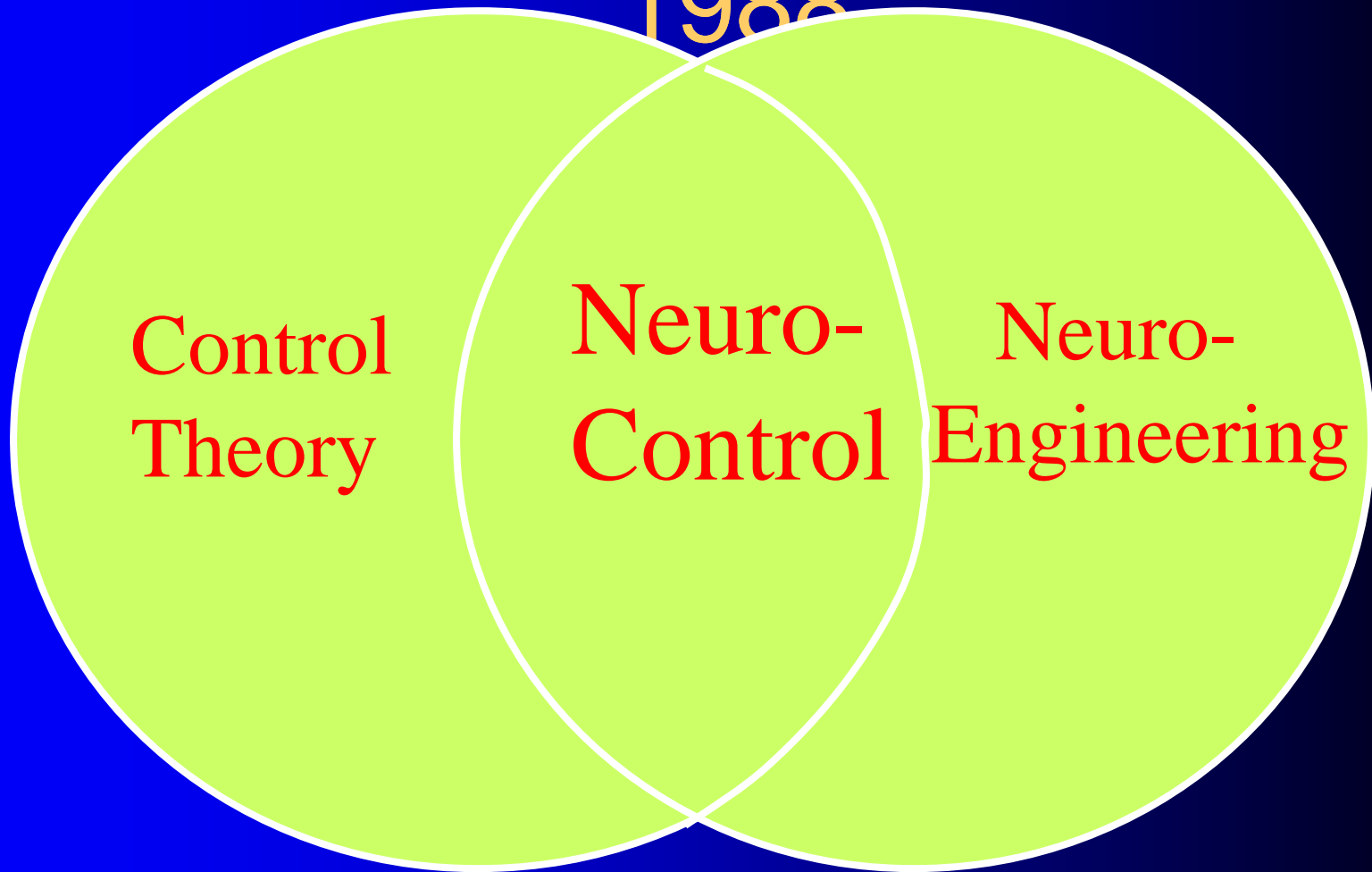
# Prediction Errors (FIC p.319)



# PURE ROBUST METHOD



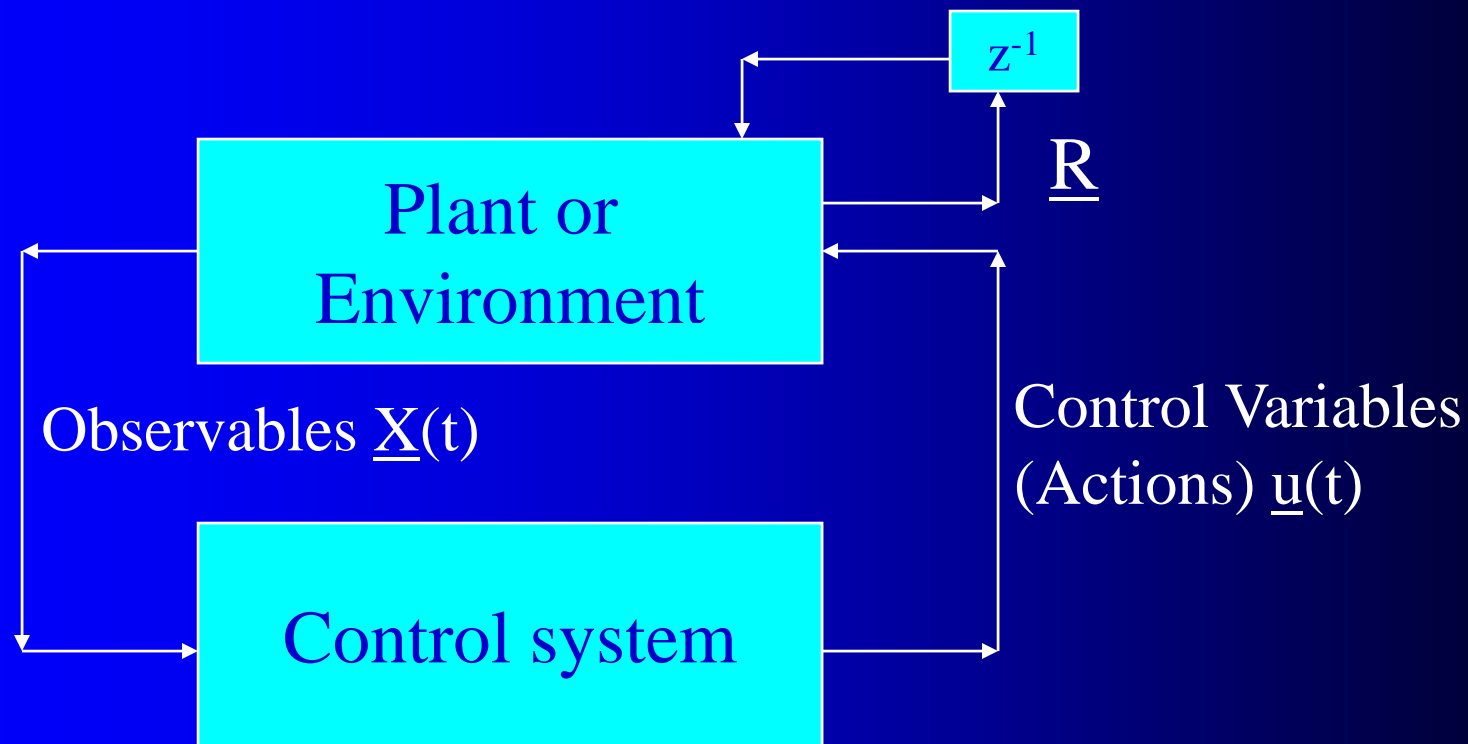
# NSF Workshop Neurocontrol 1988



Miller, Sutton, Werbos, MIT Press, 1990

**Neurocontrol is NOT JUST Control Theory!**

# What Is Control?



- $t$  may be discrete (0, 1, 2, ...) or continuous
- “Decisions” may involve multiple time scales



# Major Choices In Control (A Ladder)

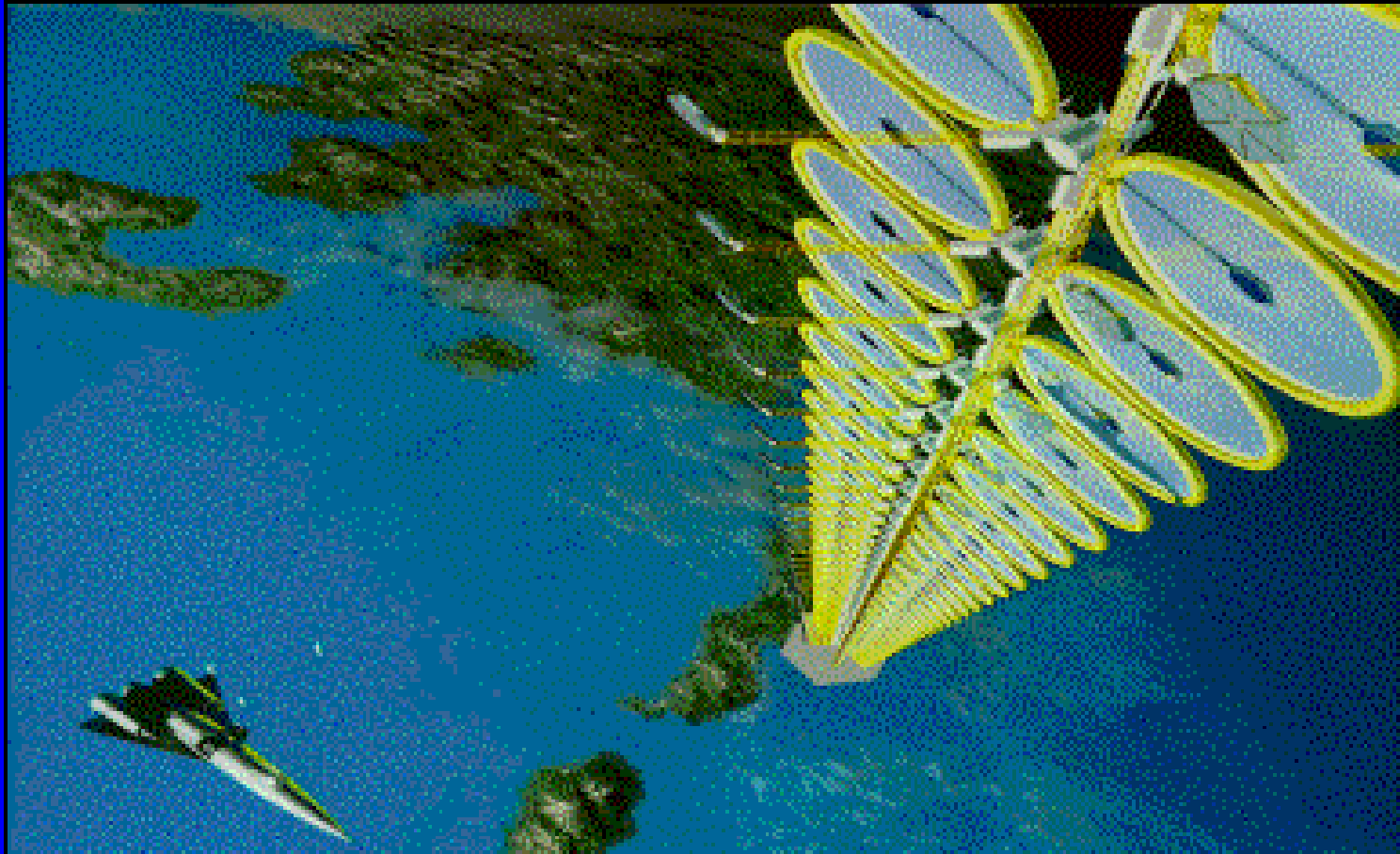
- SISO (old) versus. MIMO (modern & CI)
- Feedforward versus Feedback
- Fixed versus Adaptive versus Learning
  - e.g learn to adapt to changing road traction
- Cloning versus Tracking versus Optimization

# 3 Design

## Approaches/Goals/Tasks

- **CLONING**: Copy Expert or Other Controller
  - What the Expert Says (Fuzzy or AI)
  - What the Expert Does (Prediction of Human)
- **TRACKING**: Set Point or Reference Trajectory
  - 3 Ways to Stabilize; To Be Discussed
- **OPTIMIZATION OVER TIME**
  - n-step Lookahead vs. LQG (Stengel, Bryson/Ho)
  - vs. Approximate Dynamic Programming (Werbos)

# NSF-NASA Workshop on Learning/Robotics For Cheaper (Competitive) Solar Power



See NSF 02-098 at [www.nsf.gov](http://www.nsf.gov) &URLs



# Human mentors robot and then robot improves skill



Schaal, Atkeson  
NSF ITR project

**Learning** allowed robot to quickly learn to imitate human, and then improve agile movements (tennis strokes). **Learning** many agile movements quickly will be crucial to enabling >80% robotic assembly in space.

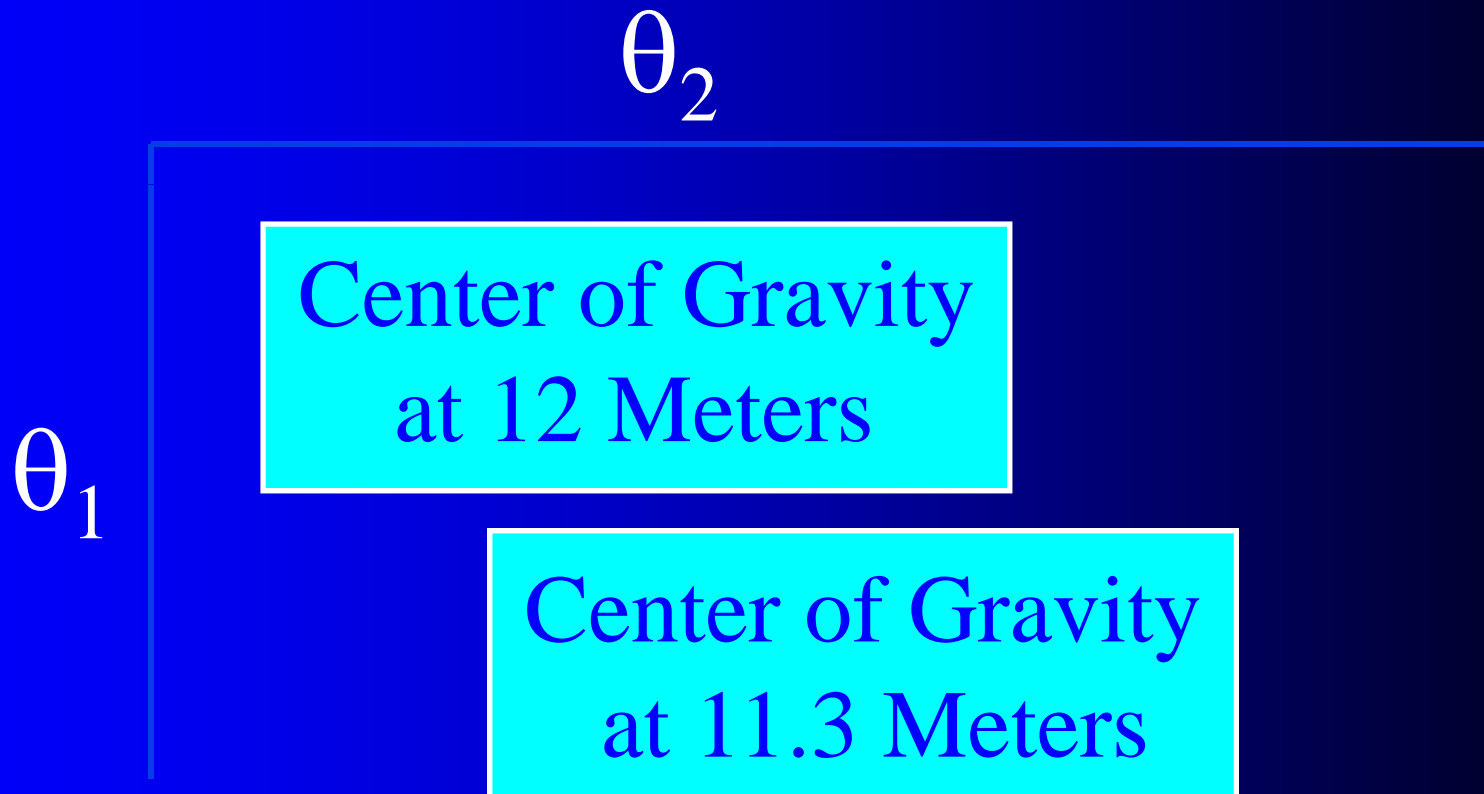
# Three Ways To Get Stability

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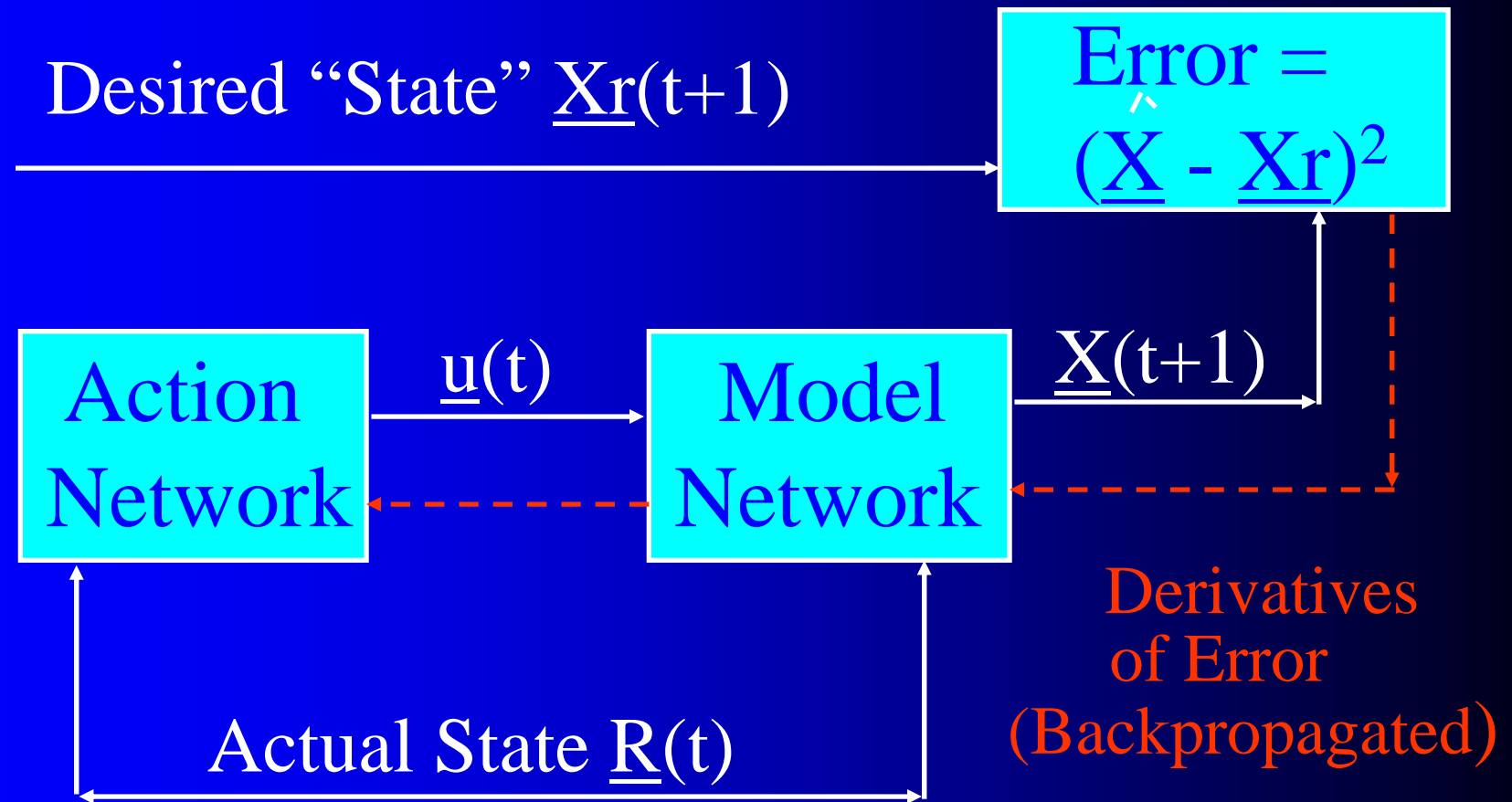
- Robust or H Infinity Control  
(Oak Tree)
- Adaptive Control (Grass)
- Learn Offline/Adaptive Online  
(Maren 90)
  - “Multistreaming” (Ford, Felkamp et al)
  - Need TLRN Controller, Noise Wrapper
  - ADP Versions: Online or “Devil Net”

# Example from Hypersonics: Parameter Ranges for Stability (Ho)

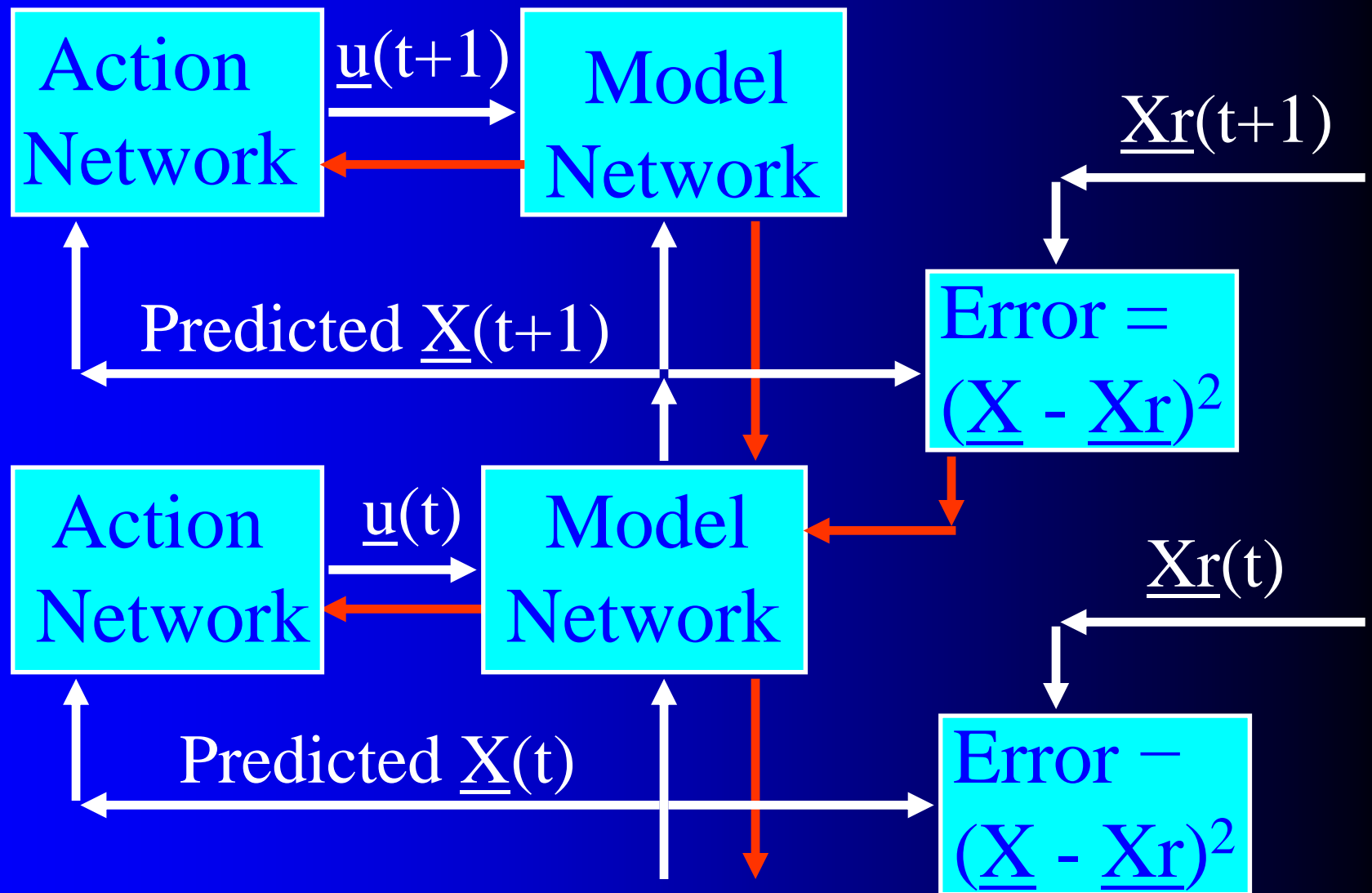
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# Idea of Indirect Adaptive Control



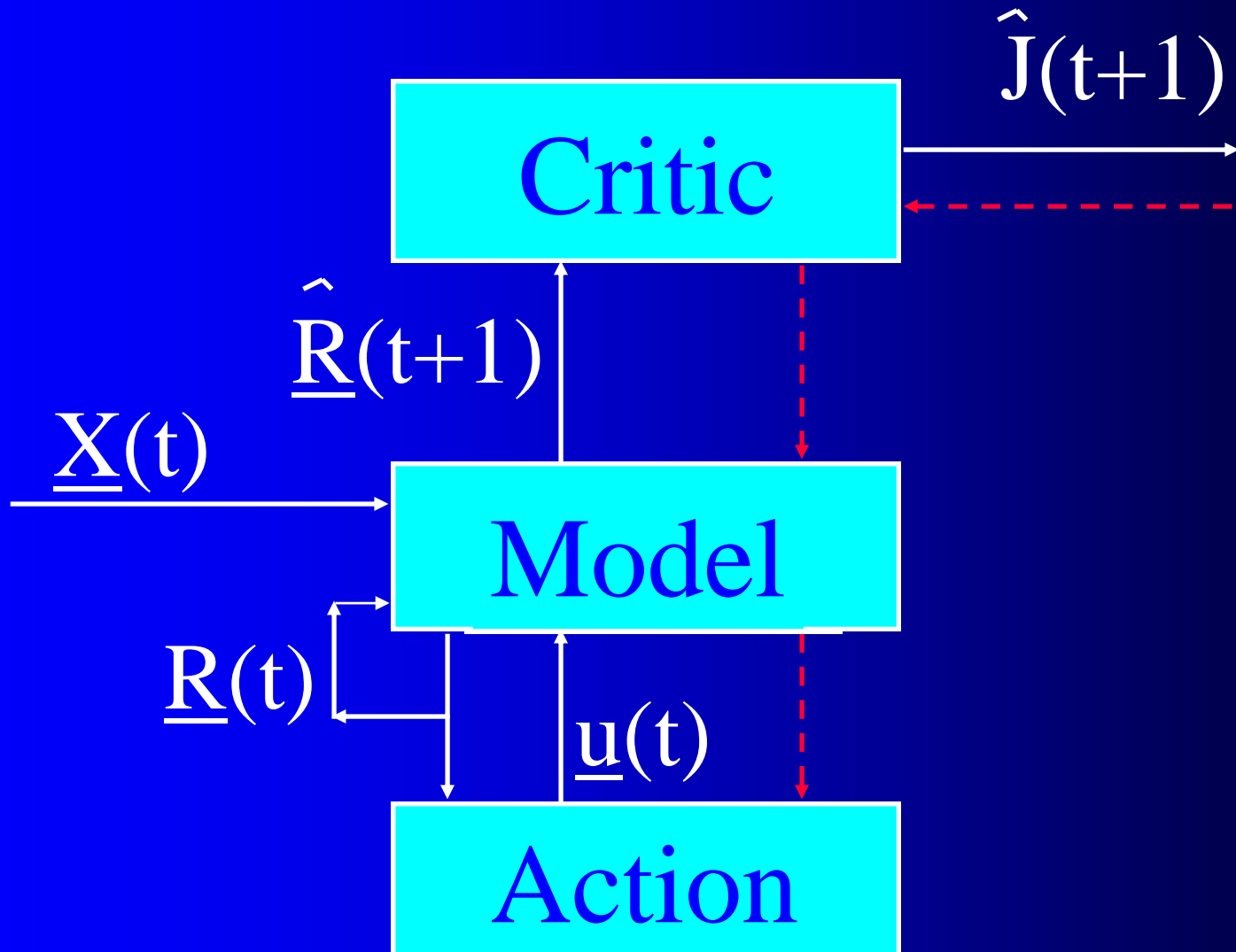
# Backpropagation Through Time (BTT) for Control (Neural MPC)



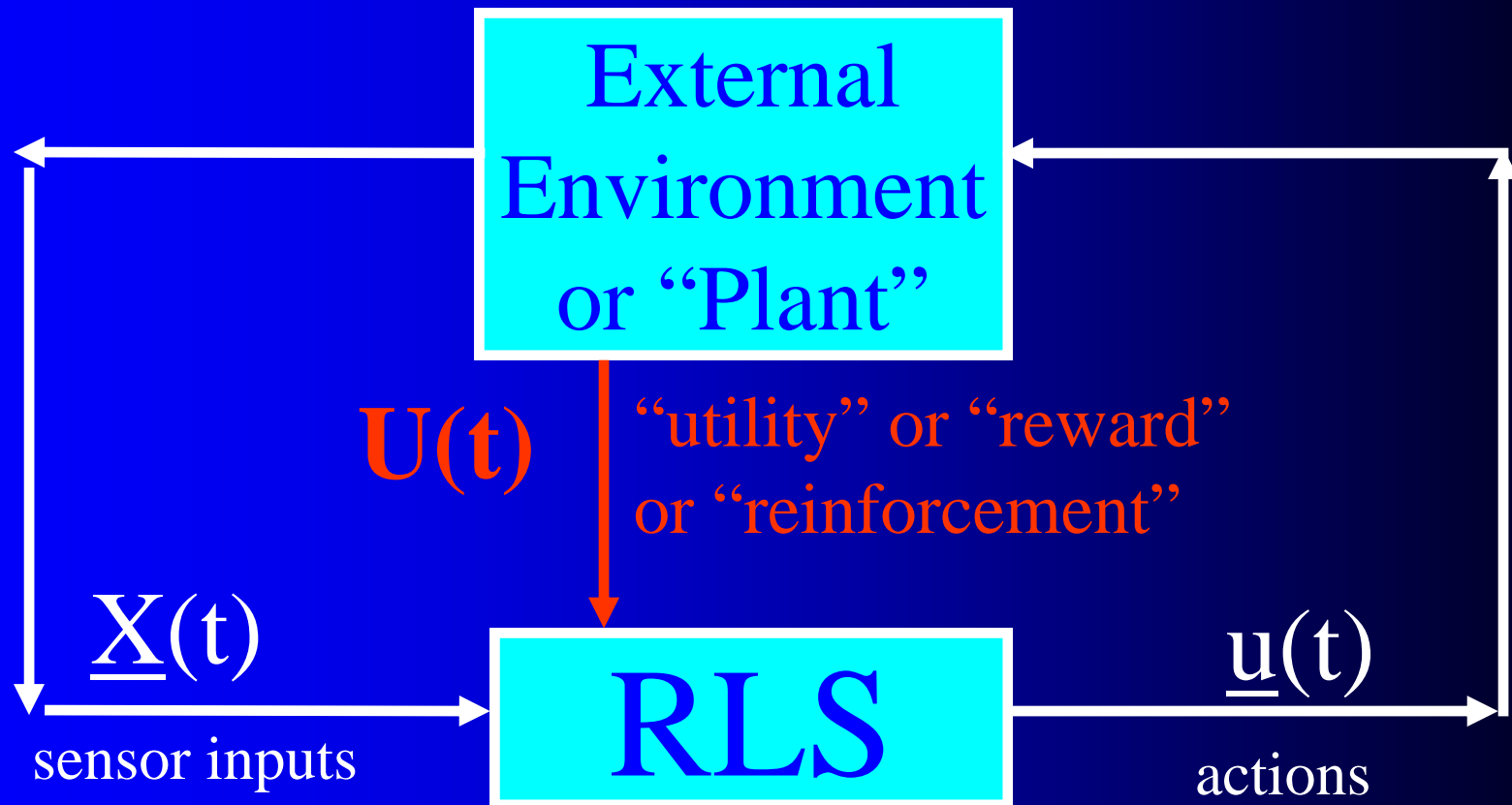


# Level 3 (HDP+BAC) Adaptive Critic System

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# Reinforcement Learning Systems (RLS)



RLS may have internal dynamics and "memory" of earlier times  $t-1$ , etc.

# Maximizing utility over time

Model of reality

Utility function  $U$

Dynamic programming

$$J(\mathbf{x}(t)) = \text{Max}_{\mathbf{u}(t)} \langle U(\mathbf{x}(t), \mathbf{u}(t)) + J(\mathbf{x}(t+1)) \rangle / (1+r)$$

Secondary, or strategic utility function  $J$



# Beyond Bellman: Learning & Approximation for Optimal Management of Larger Complex Systems

- Basic thrust is **scientific**. Bellman gives exact optima for 1 or 2 continuous state vars. New work allows 50-100 (thousands sometimes). Goal is to **scale up in space and time** -- the math we need to know to know how brains do it. And unify the recent progress.
- Low lying fruit -- missile interception, vehicle/engine control, strategic games
- **New book** from ADP02 workshop in Mexico [www.eas.asu.edu/~nsfadp](http://www.eas.asu.edu/~nsfadp) (IEEE Press, 2004, Si et al eds)

# Emerging Ways to Get Closer to Brain-Like Systems

- IEEE Computational Intelligence (CI) Society, new to 2004, about 2000 people in meetings.
- Central goal: “**end-to-end learning**” from sensors to actuators to maximize performance of plant over future, with general-purpose learning ability.
- This is DARPA’s “new **cogno**” in the new nano-info-bio-cogno convergence
- This is end-to-end cyberinfrastructure
  - See hot link at bottom of [www.eng.nsf.gov/ecs](http://www.eng.nsf.gov/ecs)
- **What’s new is a path to make it real**

# 4 Types of Adaptive Critics

- Model-free (levels 0-2)\*
  - Barto-Sutton-Anderson (BSA) design, 1983
- Model-based (levels 3-5)\*
  - Werbos Heuristic dynamic programming with backpropagated adaptive critic, 1977, Dual heuristic programming and Generalized dual heuristic programming, 1987
- Error Critic (TLRN, cerebellum models)
- 2-Brain, 3-Brain models

# Beyond Bellman: Learning & Approximation for Optimal Management of Larger Complex Systems

- Basic thrust is **scientific**. Bellman gives exact optima for 1 or 2 continuous state vars. New work allows 50-100 (thousands sometimes). Goal is to **scale up in space and time** -- the math we need to know to know how brains do it. And unify the recent progress.
- Low lying fruit -- missile interception, vehicle/engine control, strategic games
- Workshops: ADP02 in Mexico [ebrains.la.asu.edu/~nsfadp](http://ebrains.la.asu.edu/~nsfadp); coordinated workshop on anticipatory optimization for power.

# New Workshop on ADP: text/notes at

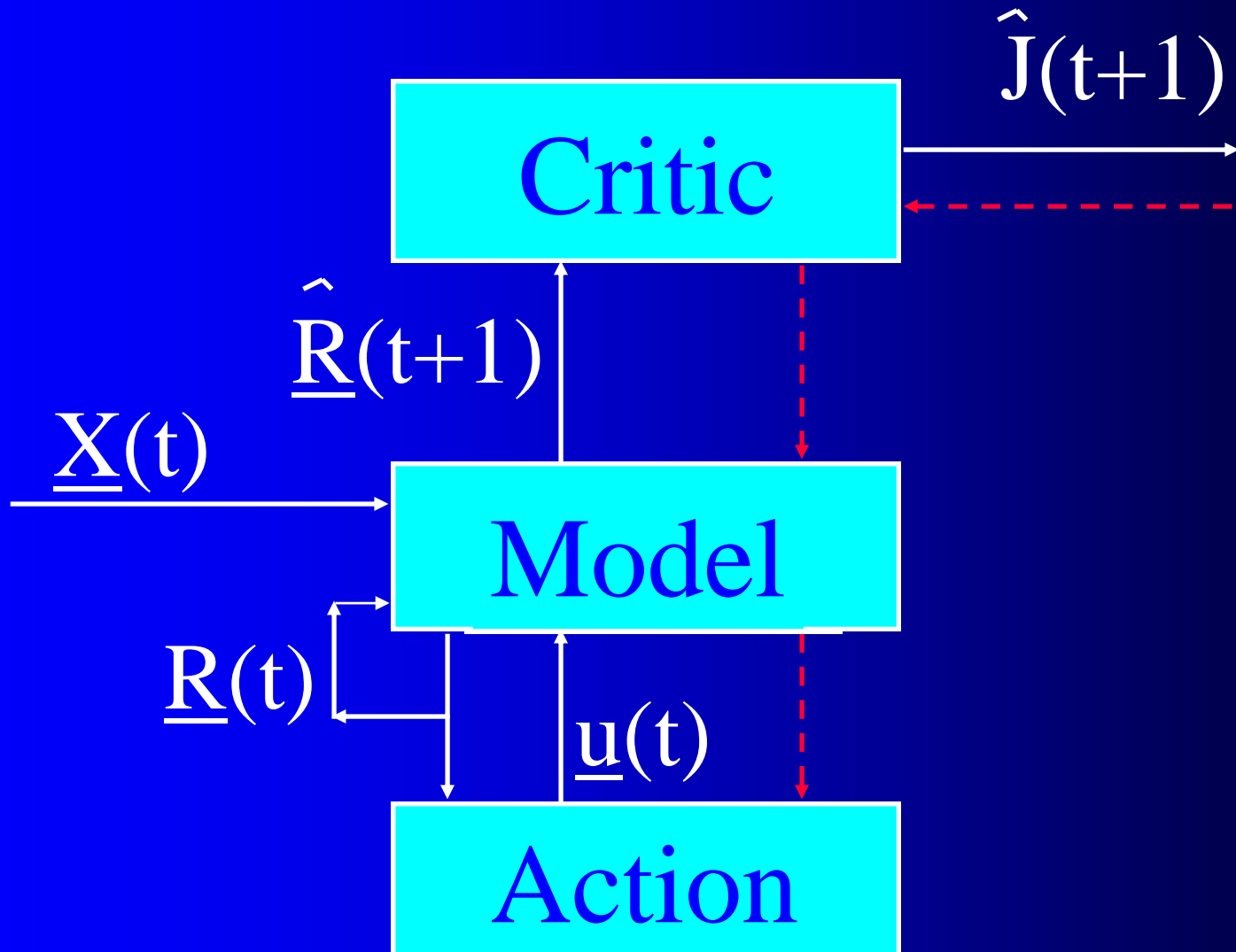
[www.eas.asu.edu/~nsfadp](http://www.eas.asu.edu/~nsfadp)

- Neural Network Engineering
  - Widrow 1st 'Critic' ('73), Werbos ADP/RL ('68-'87)
  - Wunsch, Lendaris, Balakrishnan, White, Si,LDW.....
- Control Theory
  - Ferrari/Stengel (Optimal), Sastry, Lewis, VanRoy (Bertsekas/Tsitsiklis),Nonlinear Robust...
- Computer Science/AI
  - Barto et al ('83), TD, Q, Game-Playing, .....
- Operations Research
  - Original DP: Bellman, Howard; Powell
- Fuzzy Logic/Control
  - Esogbue, Lendaris, Bien

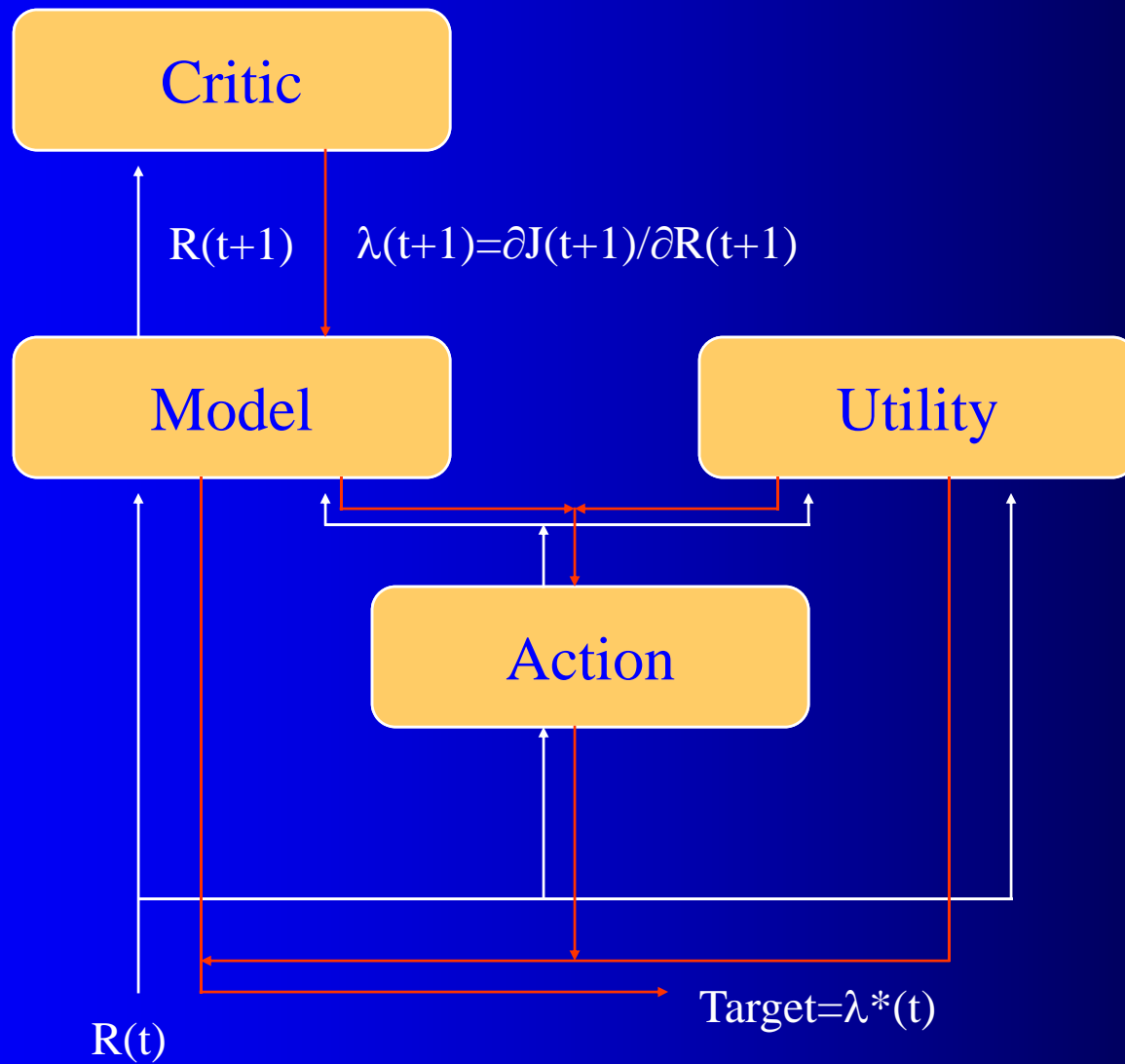


# Level 3 (HDP+BAC) Adaptive Critic System

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# Dual Heuristic Programming (DHP)



# Don Wunsch, Texas Tech ADP Turbogenerator Control CAREER 9702251, 9704734, etc.



- Stabilized voltage & reactance under intense disturbance where neuroadaptive & usual methods failed
- Being implemented in full-scale experimental grid in South Africa
- Best paper award IJCNN99

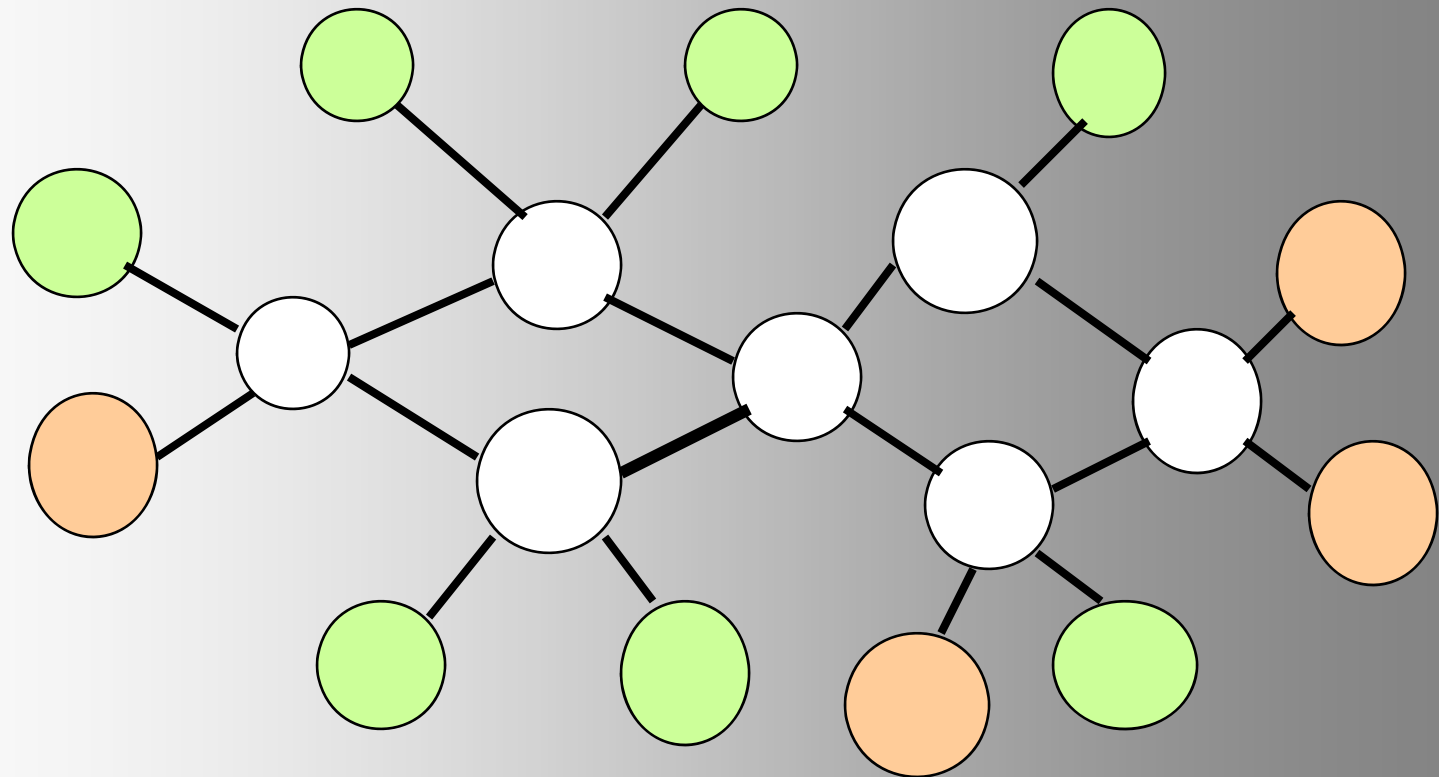
# Uses of the Main Critic Designs

- HDP=TD For DISCRETE set of Choices
- DHP when action variables  $\underline{u}$  are continuous
- GDHP when you face a mix of both (but put zero weight on undefined derivative)
- See arXiv.org , nlin-sys area, adap-org 9810001 for detailed history, equation,

# From Today's Best ADP to True (Mouse-)Brain-Like Intelligence

- ANNs For Distributed/Network I/O: “spatial chunking,” **ObjectNets**, Cellular SRNs
- Ways to Learn Levels of a Hierarchical Decision System – **Goals, Decisions**
- “Imagination” Networks, which learn from domain knowledge how to escape local optima (Brain-Like Stochastic Search BLiSS)
- Predicting True Probability Distributions

# ANN to I/O From Idealized Power Grid



- 4 General Object Types (busbar, wire, G, L)
- Net should allow **arbitrary number** of the 4 objects
- How design ANN to input and output FIELDS -- variables like the SET of values for current ACROSS all objects?

# Simple Approach to Grid-Grid Prediction in Feedforward (FF) Case

- Train 4 FF Nets, one for each TYPE of object, over all data on that object.
- E.g.: Predict Busbar(t+1) as function of Busbar(t) **and** Wire(t) for all 4 wires linked to that busbar (imposing symmetry).
- Dortmund diagnostic system uses this idea
- This IMPLICITLY defines a global FF net which inputs  $\underline{X}(t)$  and outputs grid prediction

# ObjectNets: A Recurrent Generalization (with patent)

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- **Define** a global FF Net, FF, as the combination of local object model networks, as before
- Add an auxiliary vector,  $\underline{y}$ , defined as a field over the grid (just like  $\underline{X}$  itself)
- The structure of the object net is an SRN:
  - $\underline{y}^{[k+1]} = \text{FF}(\underline{X}(t), \underline{y}^{[k]}, W)$
  - prediction (e.g.  $\underline{X}(t+1)$ ) =  $g(\underline{y}^{[\infty]})$
- Train SRNs as in [xxx.lanl.gov](http://xxx.lanl.gov), adap-org 9806001
- **General** I/O Mapping -- Key to **Value** Functions



# Four Advanced Capabilities

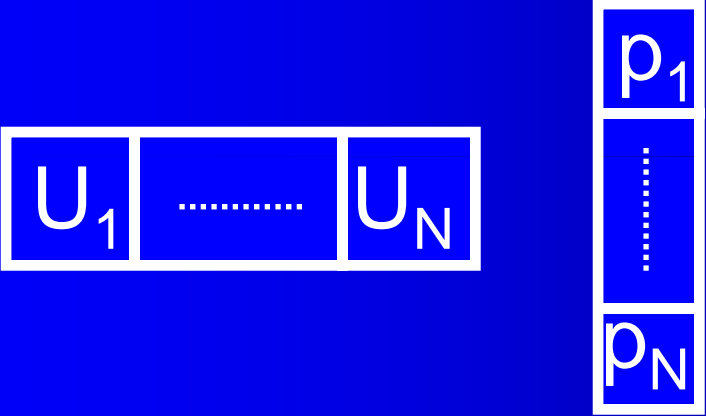
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- ANNs For Distributed/Network I/O: “spatial chunking,” ObjectNets, Cellular SRNs
- Ways to Learn Levels of a Hierarchical Decision System
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# Forms of Temporal Chunking

- Brute Force, Fixed “T”, Multiresolution
  - “Clock Based Synchronization”, NIST
  - e.g., in Go, predict 20 moves ahead
- Action Schemas or Task Modules
  - “Event Based Synchronization”: BRAIN
  - Miller/G/Pribram, Bobrow, Russell, me...

# Lookup Table Adaptive Critics 1



The diagram consists of two vectors. On the left is a horizontal vector with three cells: the first contains  $U_1$ , the second contains an ellipsis, and the third contains  $U_N$ . To its right is a vertical vector with three cells: the top contains  $p_1$ , the middle contains an ellipsis, and the bottom contains  $p_N$ .

$$\langle U(\underline{x}) \rangle =$$
$$\text{SUM (over } i) U_i p_i$$
$$= \underline{U}^T \underline{p} \text{ or } \underline{U}^T \underline{x}$$

Where  $\underline{p}_i = \Pr(X_i)$  **AND**  $M_{ij} = \Pr(X_i(t+1) \mid X_j(t))$

# Review of Lookup Table Critics 2

Bellman:  $J(\underline{x}(t)) = \langle U(\underline{x}(t)) + J(\underline{x}(t+1)) \rangle$

$$J^T \underline{x} = U^T \underline{x} + J^T M \underline{x}$$

$$J^T = U^T (I - M)^{-1}$$

# Learning Speed of Critics...

- Usual Way:  $J^{(0)} = U$ ,  $J^{(n+1)} = U + M^T J^{(n)}$ 
  - After  $n$  iterations,  $J(t)$  approximates
  - $U(t) + U(t+1) + \dots + U(t+n)$
- DOUBLING TRICK shows one can be faster:  $J^T = U^T (I+M) (I+M^2) (I+M^4) \dots$ 
  - After  $n$  BIG iterations,  $J(t)$  approximates
  - $U(t) + U(t+1) + \dots + U(t+2^n)$

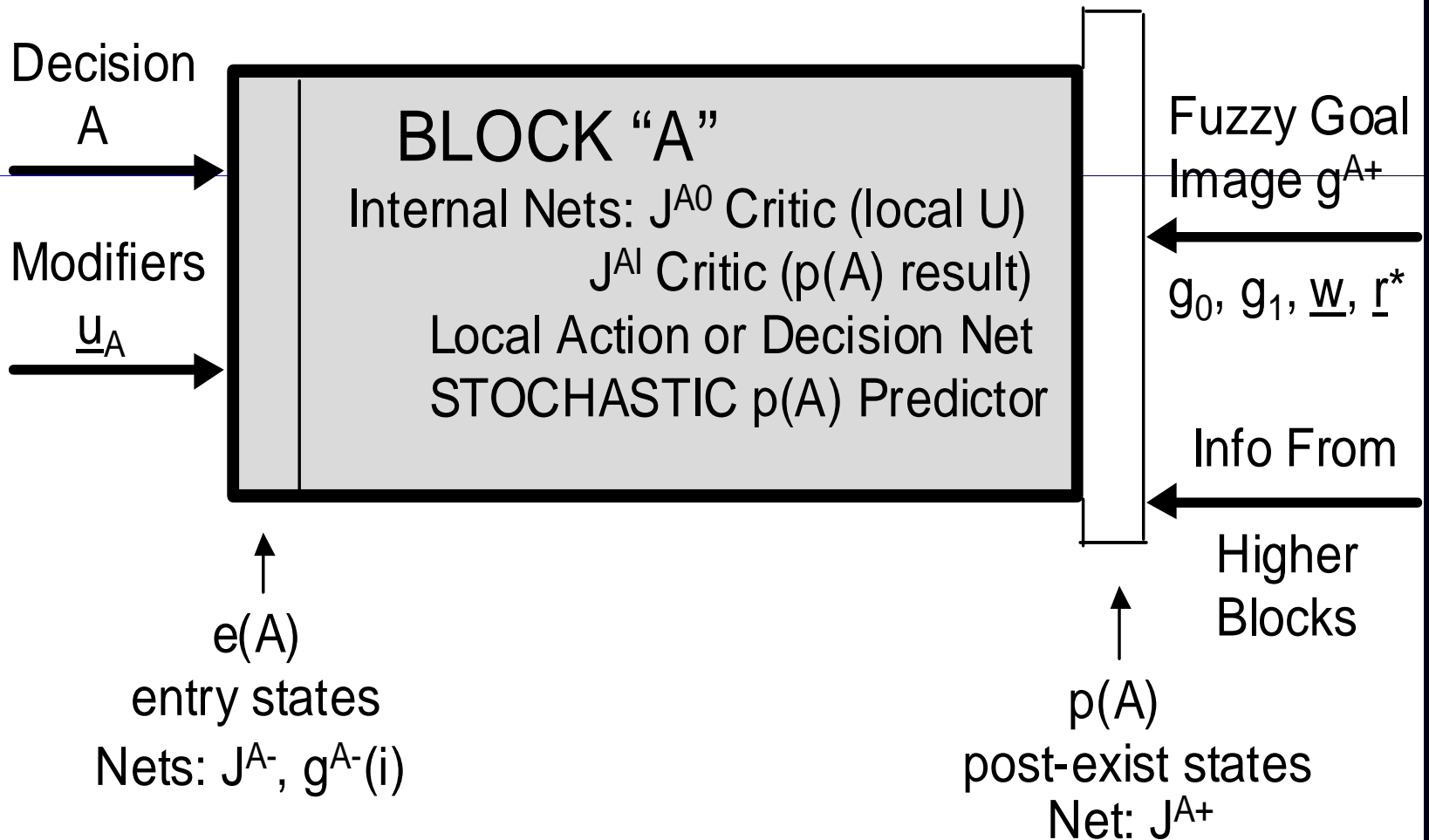
# But: What if M is Sparse, Block Structured, and Big??

- M-to-the-2-to-the-nth Becomes a MESS
- Instead use the following equation, the key result for the flat lookup table case:

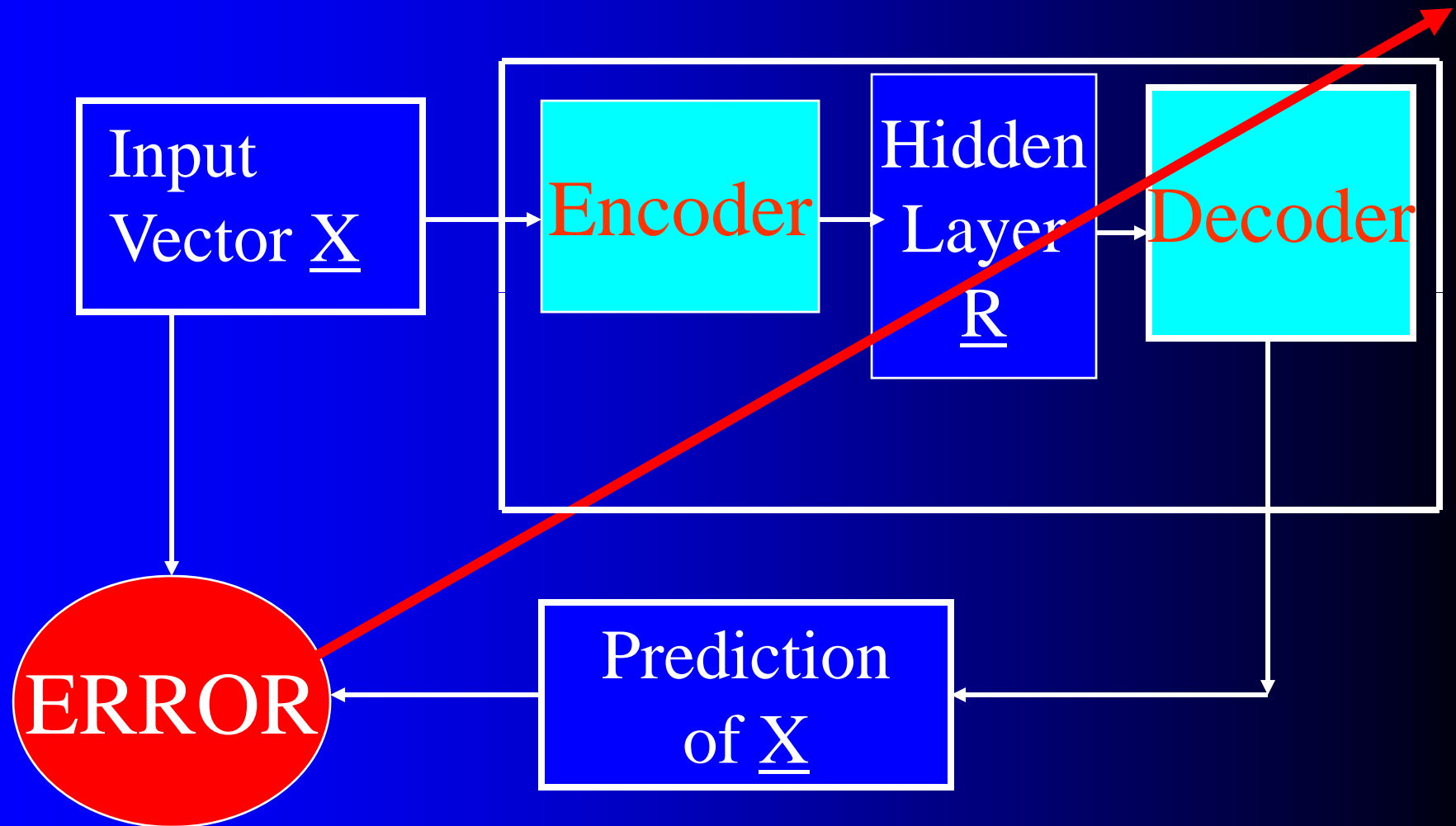
$$J_i^T = (J_i^A)^T + \text{SUM (over } j \text{ in } N(i)) J_j^T (J^B)_{ij}$$

where  $J^A$  represents utility within valley  $i$  before exit, and  $J^B$  works back utility from the exits in New valleys  $j$  within the set of possible next valleys  $N(i)$

# Structure of a Decision Block

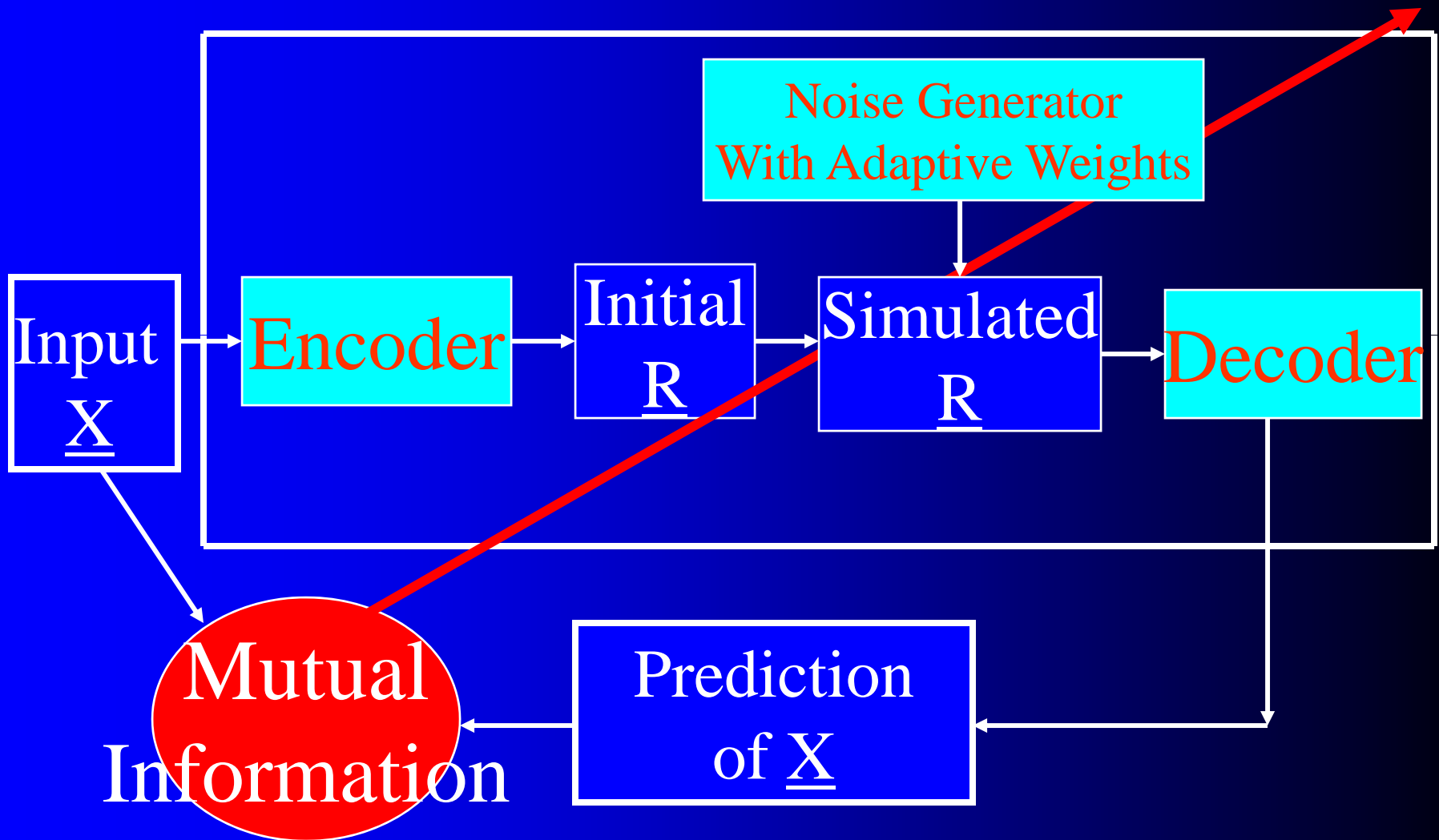


# Conventional Encoder/Decoder ("PCA")





# Stochastic ED (See HIC Ch. 13)



Full Design Also Does the Dynamics Right

